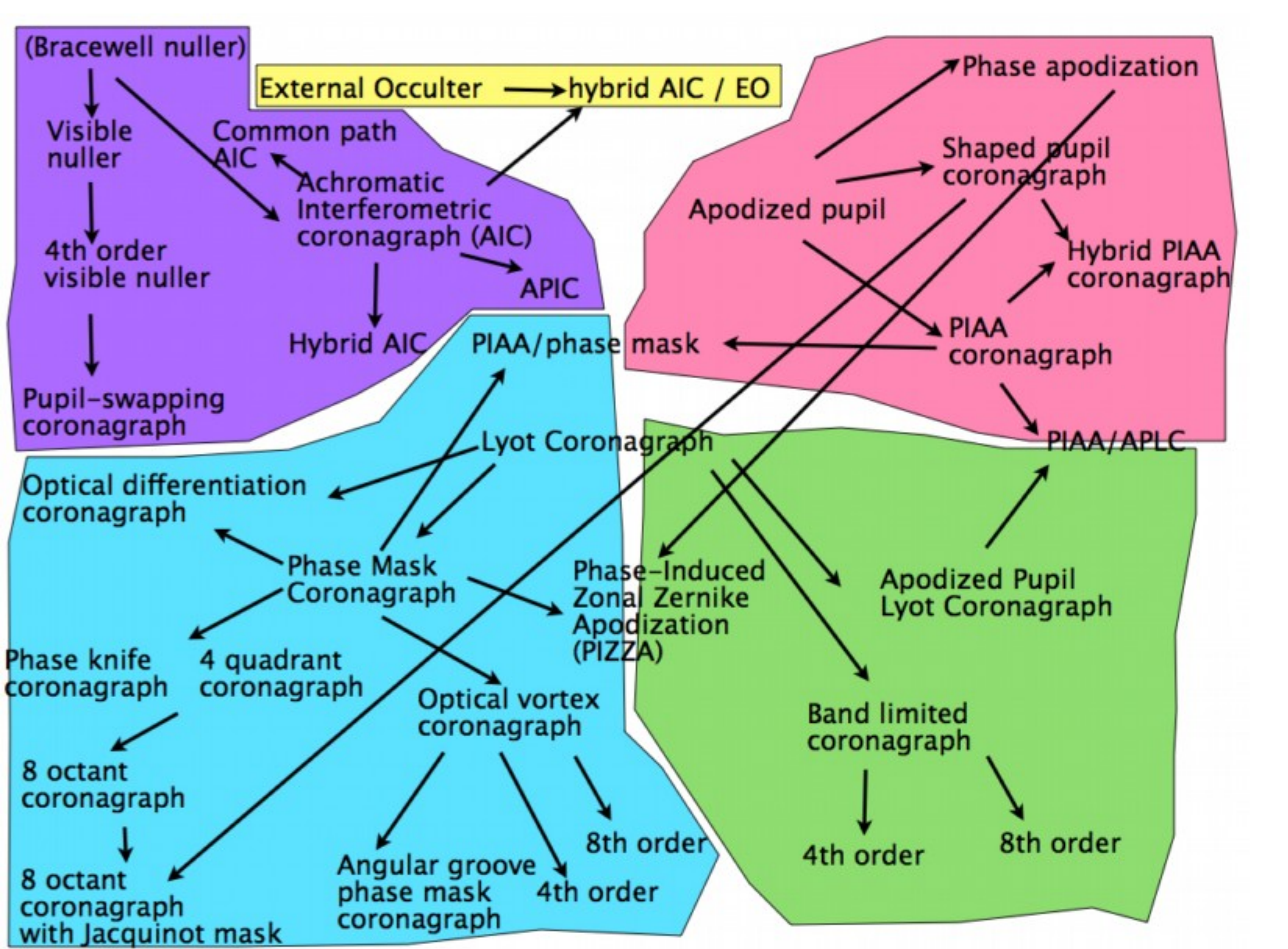


Coronagraph concepts & systems

Types of coronagraphs

Coronagraph systems & instruments





Lyot Coronagraph explained by Fourier transforms

Pupil plane complex amplitude $\leftrightarrow$ focal plane complex amplitude

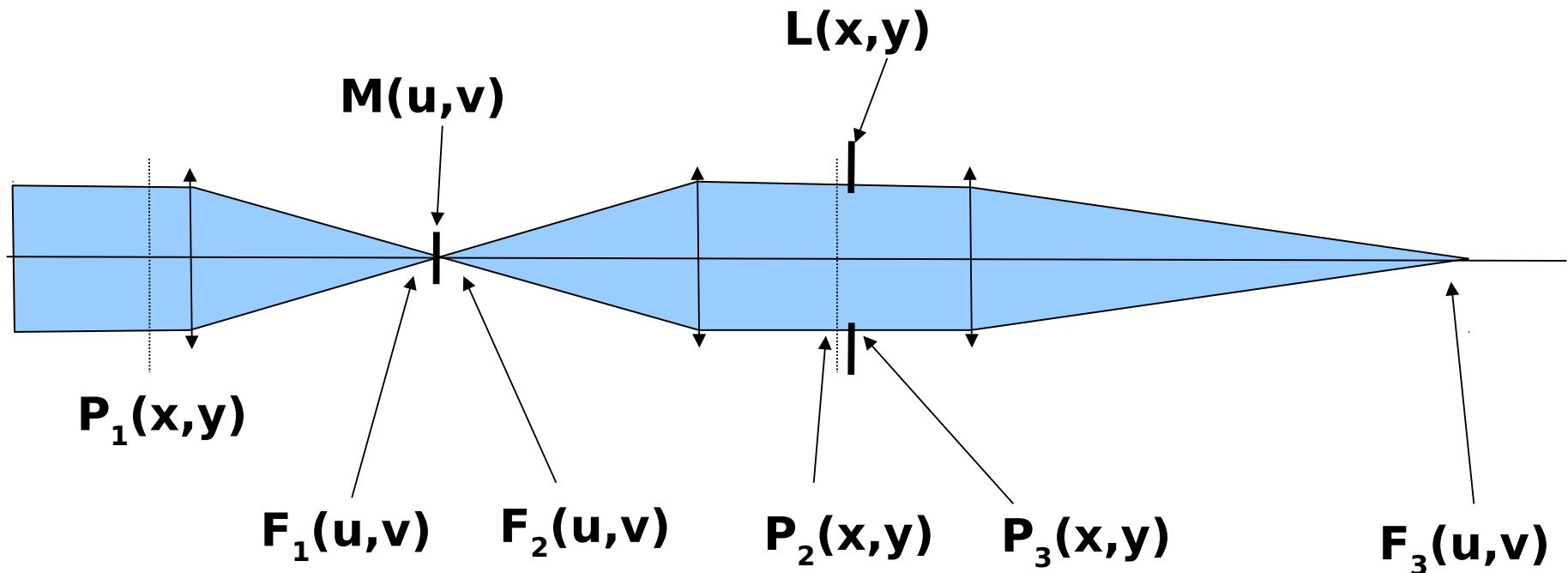
$\rightarrow$ Fourier transform

$\leftarrow$ Inverse Fourier transform

Coordinates in pupil plane: x, y

Coordinates in focal plane : u, v

* denoting convolution (product = convolution in Fourier transform)



Lyot Coronagraph explained by Fourier transforms

Full set of equations (explained in next slides):

Entrance pupil of telescope: $P_1(x,y)$

Focal plane complex amplitude (before focal plane mask): $F_1(u,v)$

$$F_1(u,v) = \text{FT} (P_1(x,y))$$

Focal plane mask complex amplitude transmission: $M(u,v)$

Focal plane complex amplitude (after focal plane mask): $F_2(u,v)$

$$F_2(u,v) = F_1(u,v) \times M(u,v) = \text{FT}(P_1(x,y)) \times M(u,v)$$

Exit pupil plane:

$$P_2(x,y) = \text{FT}^{-1}(F_2(u,v)) = \text{FT}^{-1} (\text{FT}(P_1(x,y)) \times M(u,v)) = P_1(x,y) * \text{FT}^{-1}(M(u,v))$$

With * denoting convolution

$$P_3(x,y) = L(x,y) \times P_2(x,y)$$

$$\mathbf{P_3(x,y) = L(x,y) \times (P_1(x,y) * FT^{-1}(M(u,v)))}$$

$$F_3(u,v) = \text{FT}(L(x,y)) * (F_1(u,v) \times M(u,v))$$

Coronagraphy problem: minimize $P_3(x,y)$ for on-axis point source

Lyot Coronagraph explained by Fourier transforms

Pupil plane complex amplitude $\leftrightarrow$ focal plane complex amplitude

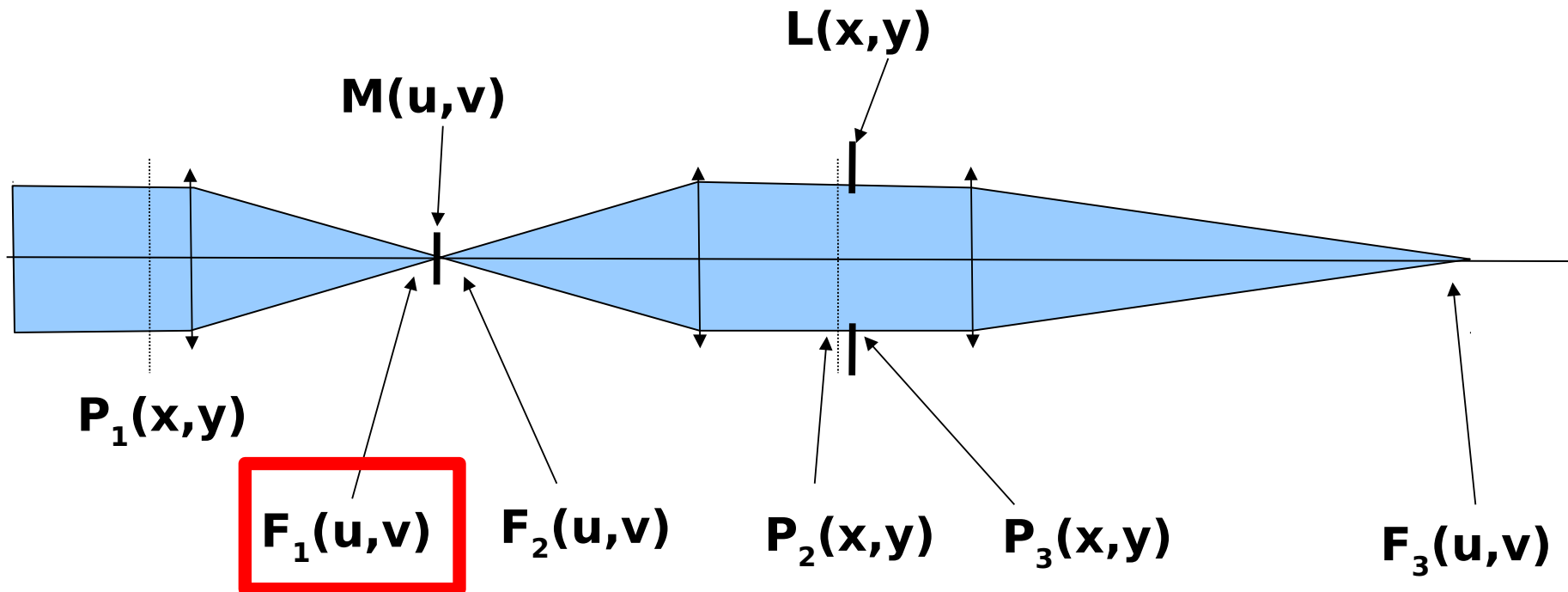
$\rightarrow$ Fourier transform

$\leftarrow$ Inverse Fourier transform

Coordinates in pupil plane: x, y

Coordinates in focal plane : u, v

* denoting convolution (product = convolution in Fourier transform)

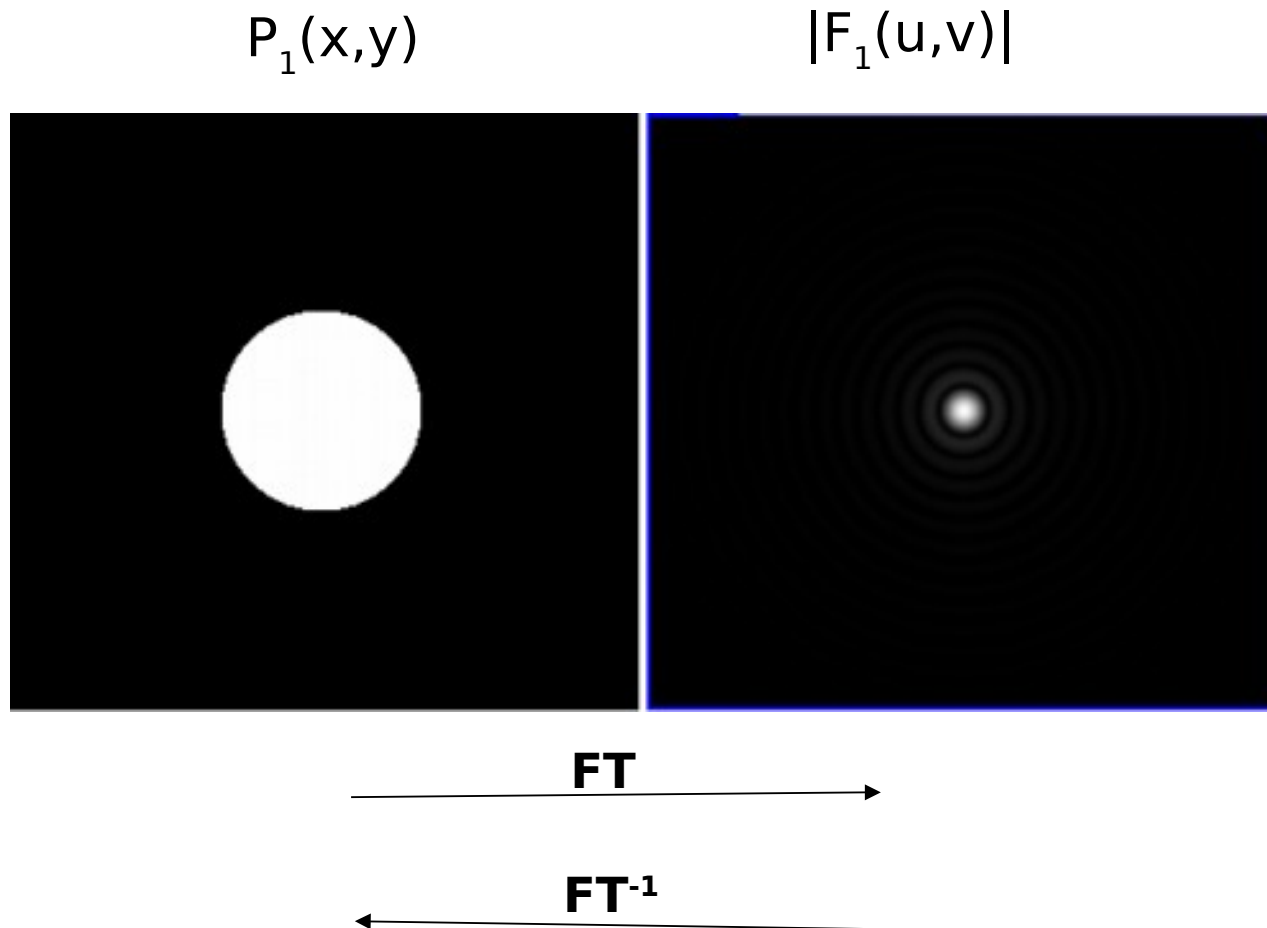


Focal plane image = FT of pupil complex amplitude

Entrance pupil of telescope: $P_1(x,y)$

Focal plane complex amplitude (before focal plane mask): $F_1(u,v)$

$$F_1(u,v) = \text{FT} (P_1(x,y))$$



Lyot Coronagraph explained by Fourier transforms

Pupil plane complex amplitude $\leftrightarrow$ focal plane complex amplitude

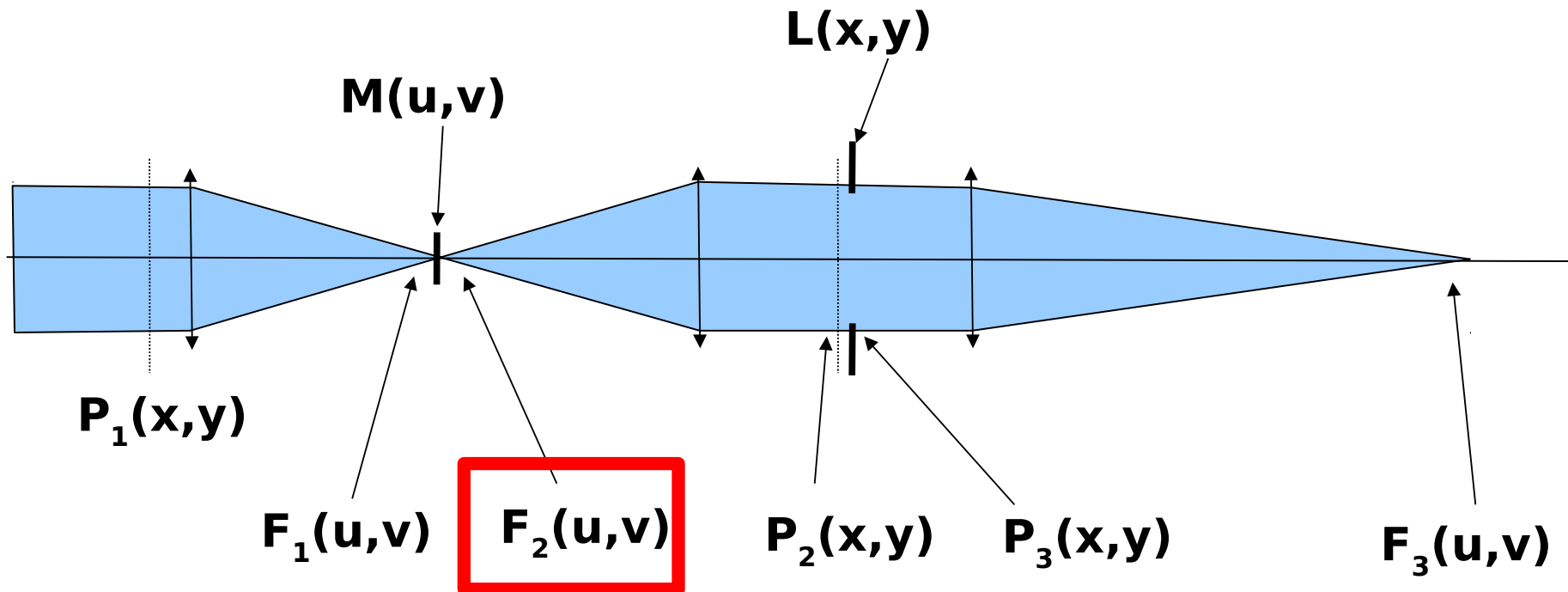
$\rightarrow$ Fourier transform

$\leftarrow$ Inverse Fourier transform

Coordinates in pupil plane: x, y

Coordinates in focal plane : u, v

* denoting convolution (product = convolution in Fourier transform)

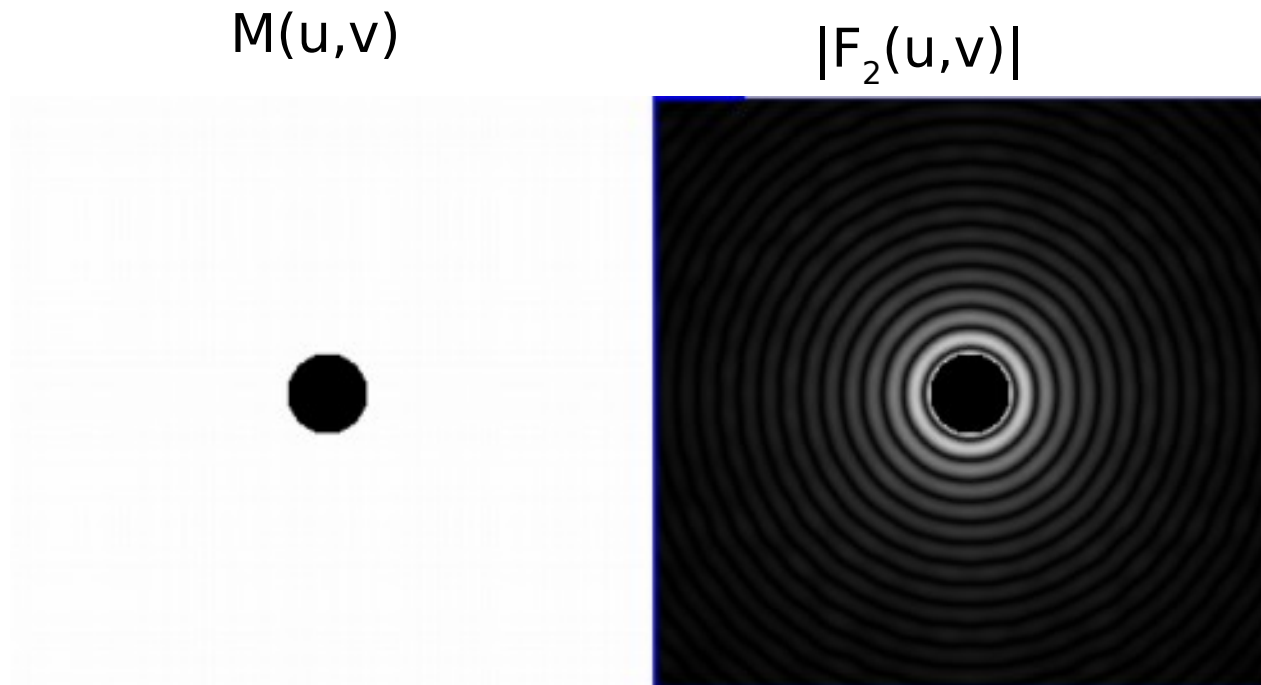


Inserting an opaque mask in the focal plane

Focal plane mask complex amplitude transmission: $M(u,v)$

Focal plane complex amplitude (after focal plane mask): $F_2(u,v)$

$$F_2(u,v) = F_1(u,v) \times M(u,v) = \text{FT}(P_1(x,y)) \times M(u,v)$$



Lyot Coronagraph explained by Fourier transforms

Pupil plane complex amplitude $\leftrightarrow$ focal plane complex amplitude

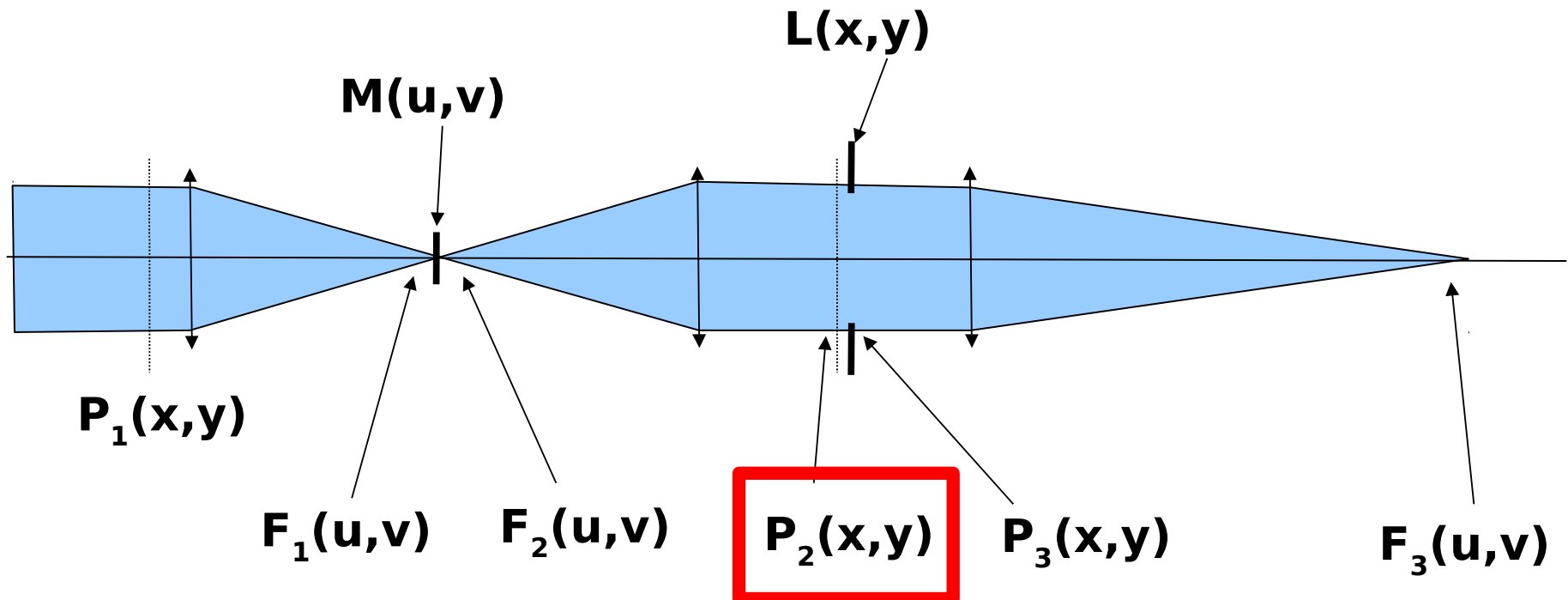
$\rightarrow$ Fourier transform

$\leftarrow$ Inverse Fourier transform

Coordinates in pupil plane: x, y

Coordinates in focal plane : u, v

* denoting convolution (product = convolution in Fourier transform)



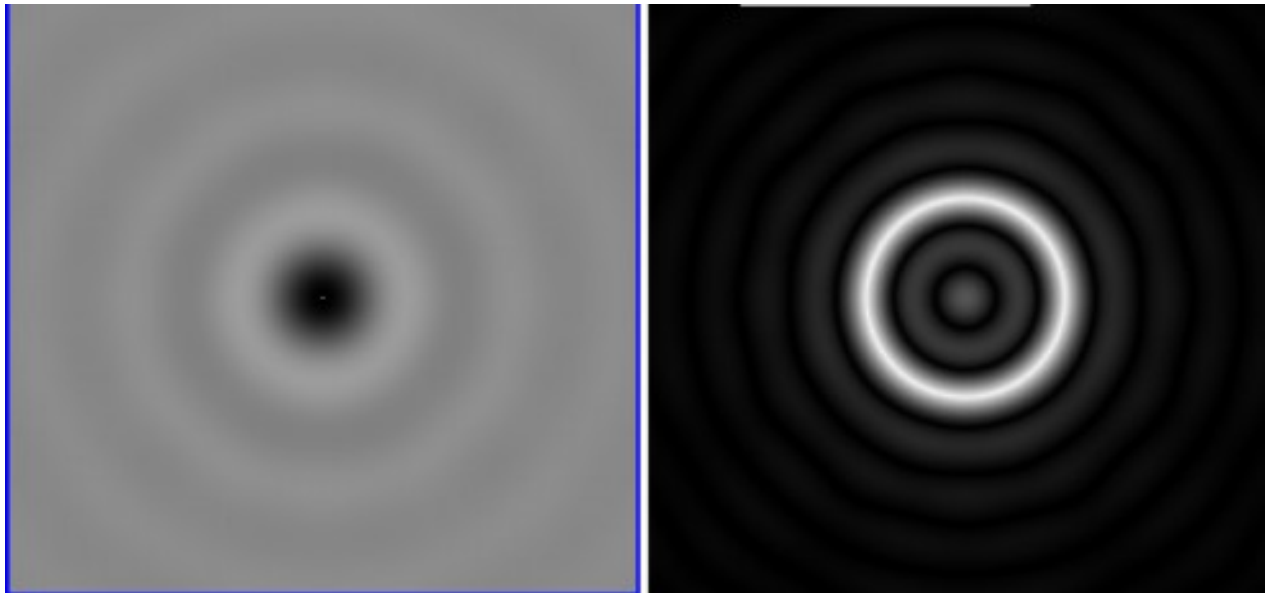
Lyot Coronagraph : light distribution in output pupil plane

Exit pupil plane:

$$\begin{aligned} P_2(x,y) &= \text{FT}^{-1}(F_2(u,v)) \\ &= \text{FT}^{-1} (\text{FT}(P_1(x,y) \times M(u,v))) = P_1(x,y) * \text{FT}^{-1}(M(u,v)) \end{aligned}$$

$\text{FT}^{-1}(M(u,v))$

$|P_2(x,y)|$



Lyot Coronagraph explained by Fourier transforms

Pupil plane complex amplitude $\leftrightarrow$ focal plane complex amplitude

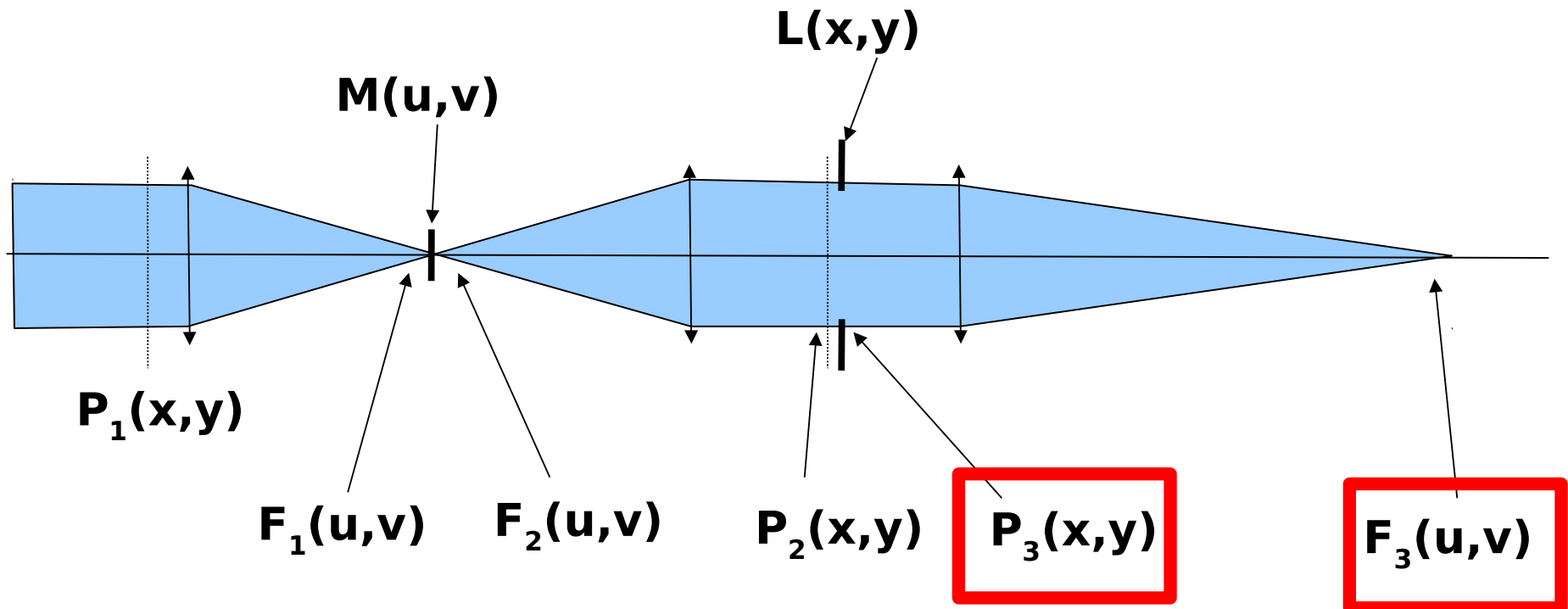
$\rightarrow$ Fourier transform

$\leftarrow$ Inverse Fourier transform

Coordinates in pupil plane: x, y

Coordinates in focal plane : u, v

* denoting convolution (product = convolution in Fourier transform)



Lyot Coronagraph : Lyot stop (L)

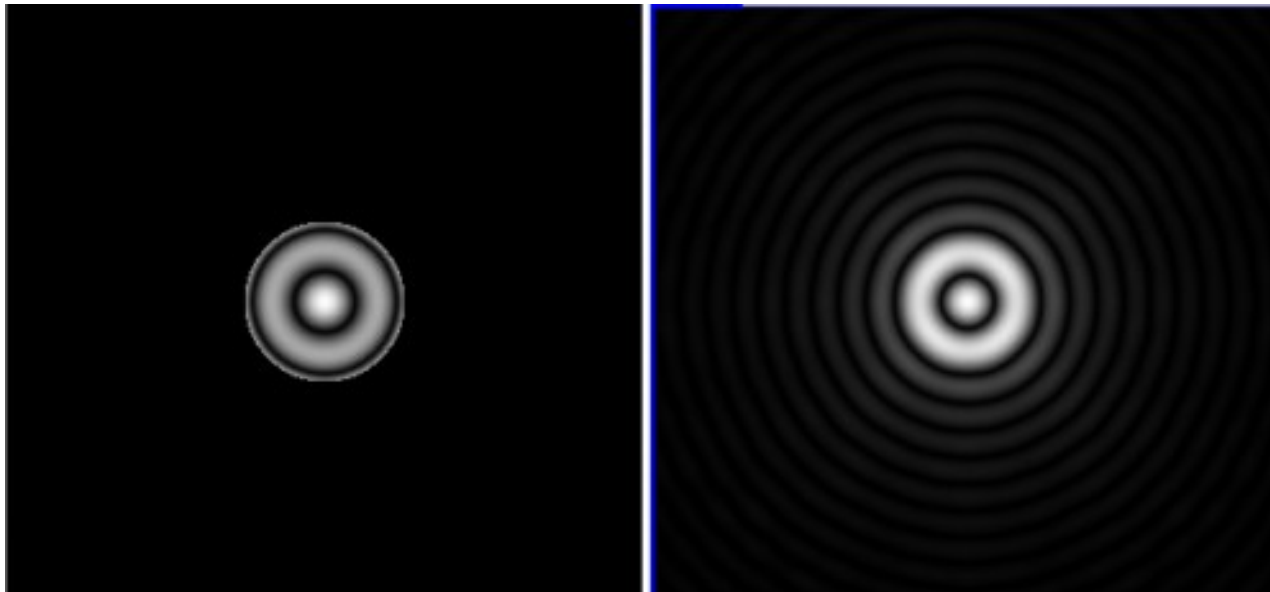
$$P_3(x,y) = L(x,y) \times P_2(x,y)$$

$$\mathbf{P}_3(\mathbf{x},\mathbf{y}) = \mathbf{L}(\mathbf{x},\mathbf{y}) \times (\mathbf{P}_1(\mathbf{x},\mathbf{y}) * \mathbf{FT}^{-1}(\mathbf{M}(\mathbf{u},\mathbf{v})))$$

$$F_3(u,v) = \mathbf{FT}(L(x,y)) * (F_1(u,v) \times M(u,v))$$

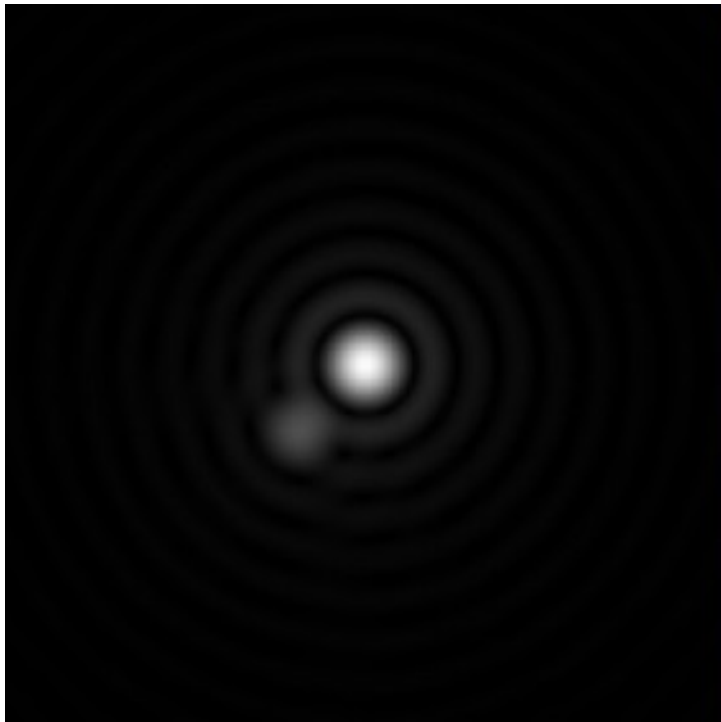
$|P_3(x,y)|$

$|F_3(u,v)|$

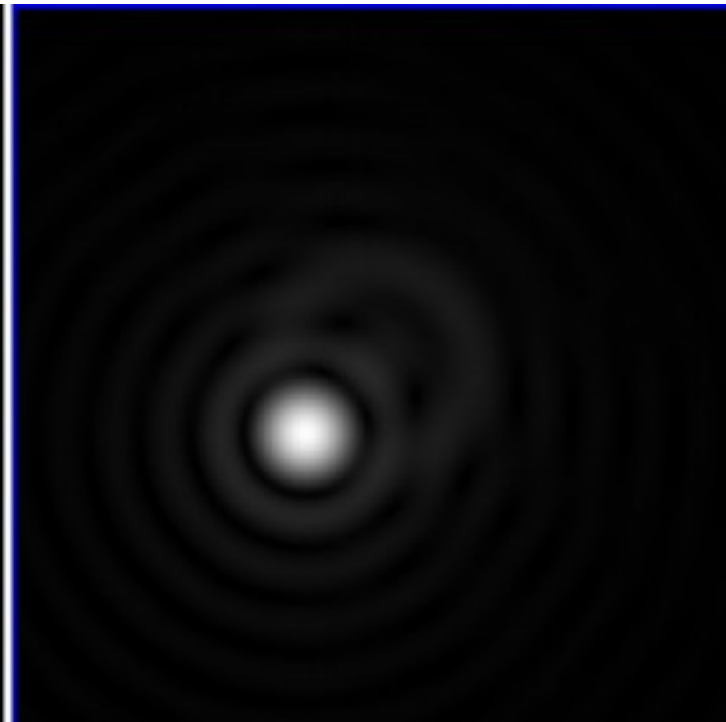


Numerical simulation of final image for 10:1 contrast

No coronagraph



With Lyot
Coronagraph



Lyot Coronagraph : optimizations

Conventional Lyot coronagraph is limited in performance:

- cannot reach extremely high contrast (some light in pupil)
- tradeoff between throughput and contrast
- not able to get high contrast close to the optical axis

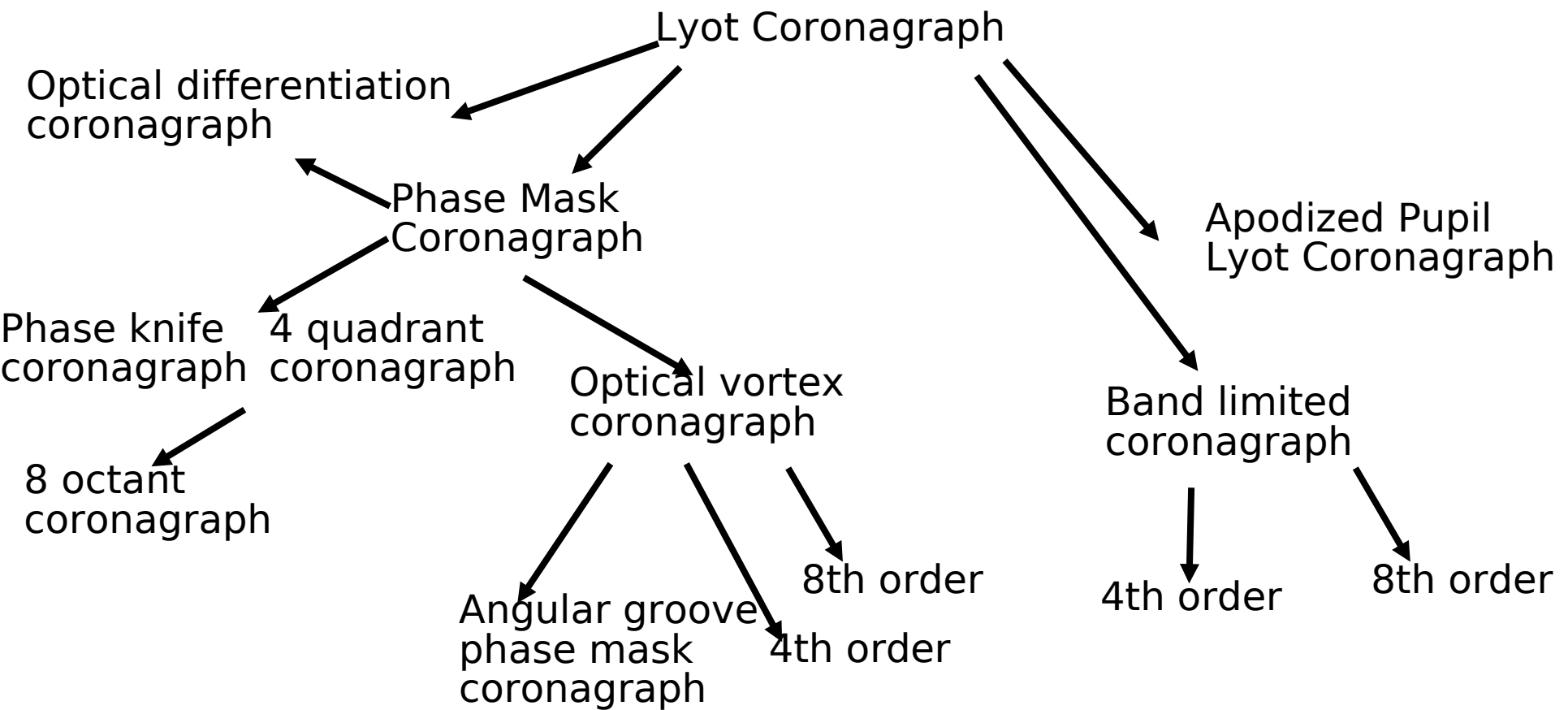
Optimization goal: make pupil dark inside Lyot mask

Possible optimizations include:

(1) Redesign of focal plane mask

- Band-limited
- Use phase as well as (or instead of) amplitude

(2) Apodize entrance aperture



Pupil Apodization

Since Airy rings originate from sharp edges of the pupil, why not change the pupil ?

Conventional Pupil Apodization/ Shaped pupil

CPA

[Kasdin et al. 2003](#)

Make the pupil edges fainter by absorbing light, either with a continuous or "binary" (shaped pupil) mask

Achromatic Pupil Phase Apodization

PPA

[Yang & Kostinski, 2004](#)

Same as CPA, but achieved by a phase apodization rather than amplitude

Phase Induced Amplitude Apodization Coronagraph PIAAC

[Guyon, 2003](#)

Perform amplitude apodization by remapping of the pupil with aspheric optics

Phase Induced Zonal Zernike Apodization

PIZZA

[Martinache, 2003](#)

Transform a pupil phase offset into an amplitude apodization thanks to a focal plane Zernike mask

Conventional Pupil Apodization (CPA)

Many pupil apodizations have been proposed.

Apodization can be continuous or binary.

- + Simple, robust, achromatic
- low efficiency for high contrast

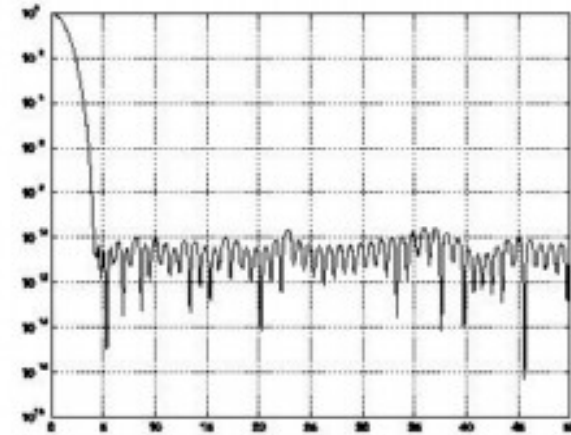
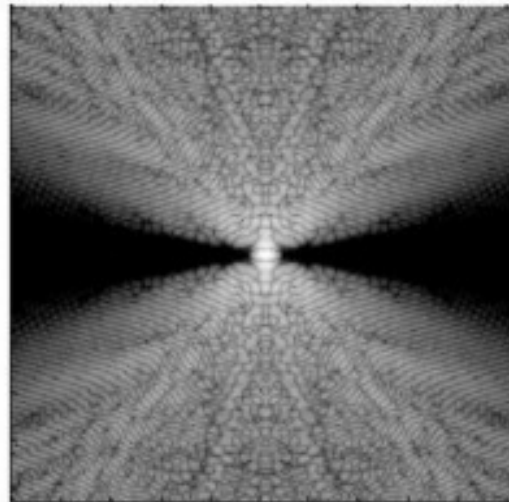
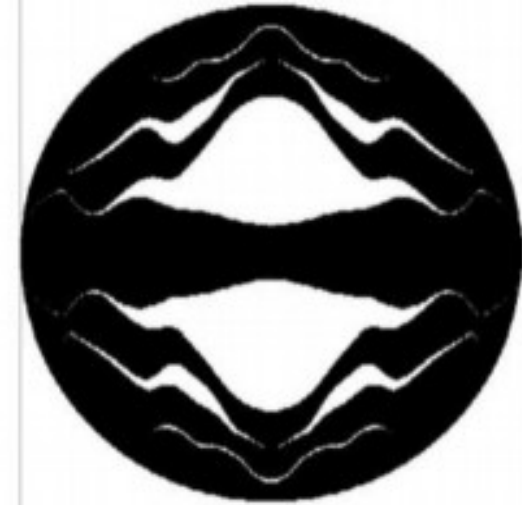
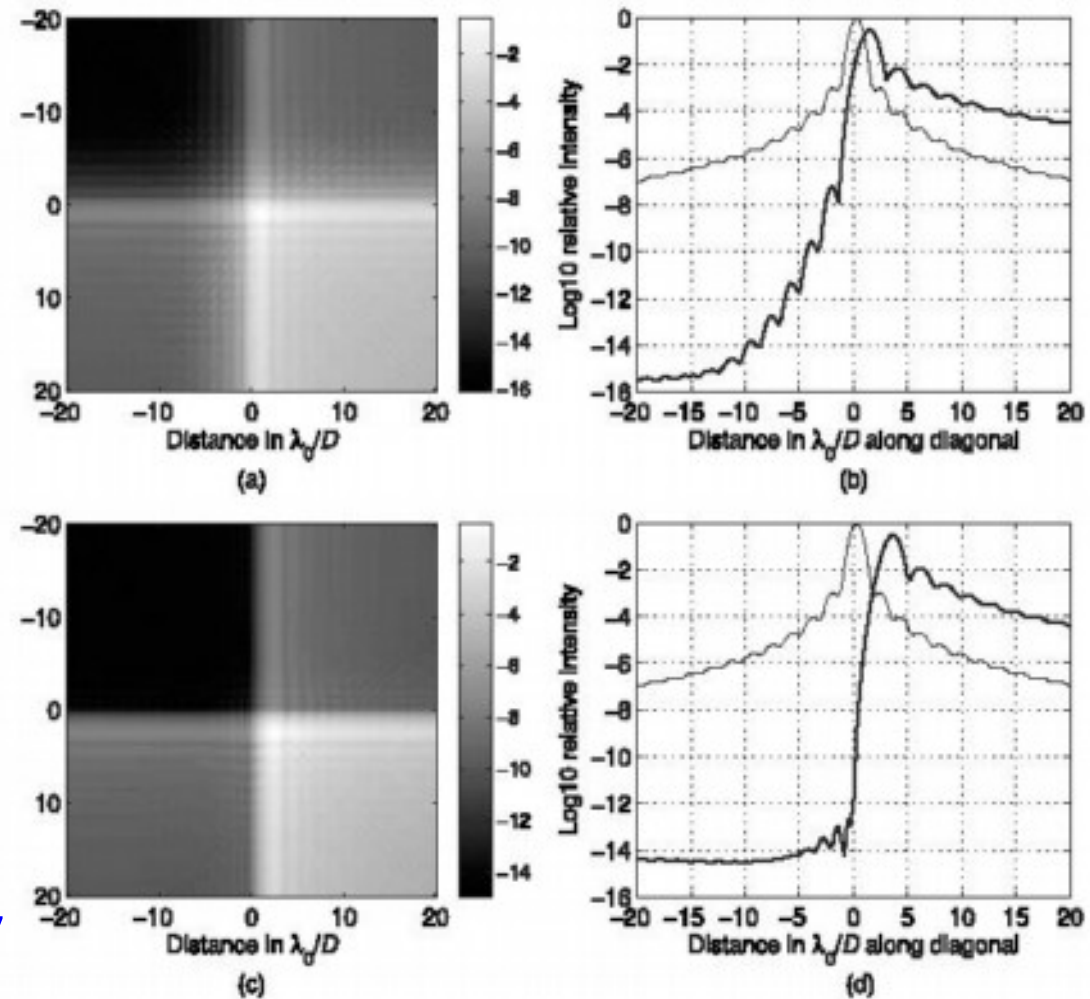


Fig. 9.—Top: Asymmetric multiopening mask designed to provide high-contrast, 10^{-10} , from $\lambda/D = 4$ to $\lambda/D = 100$ in two angular sectors centered on the x-axis. Ten integrations are required to cover all angles. Total throughput and pseudoarea are 24.4%. Airy throughput is 11.85%. Bottom: Associated PSF. (Note that this mask was originally designed for an elliptical mirror. It has been rescaled to fit a circular aperture.)

Jacquinot & Roisin-Dossier 1964
Kasdin et al. 2003, ApJ, 582, 1147
Vanderbei et al. 2003, ApJ, 590, 593
Vanderbei et al. 2003, ApJ, 599, 686
Vanderbei et al. 2004, ApJ, 615, 555

Pupil Phase Apodization (PPA)

Achromatic solutions exist.

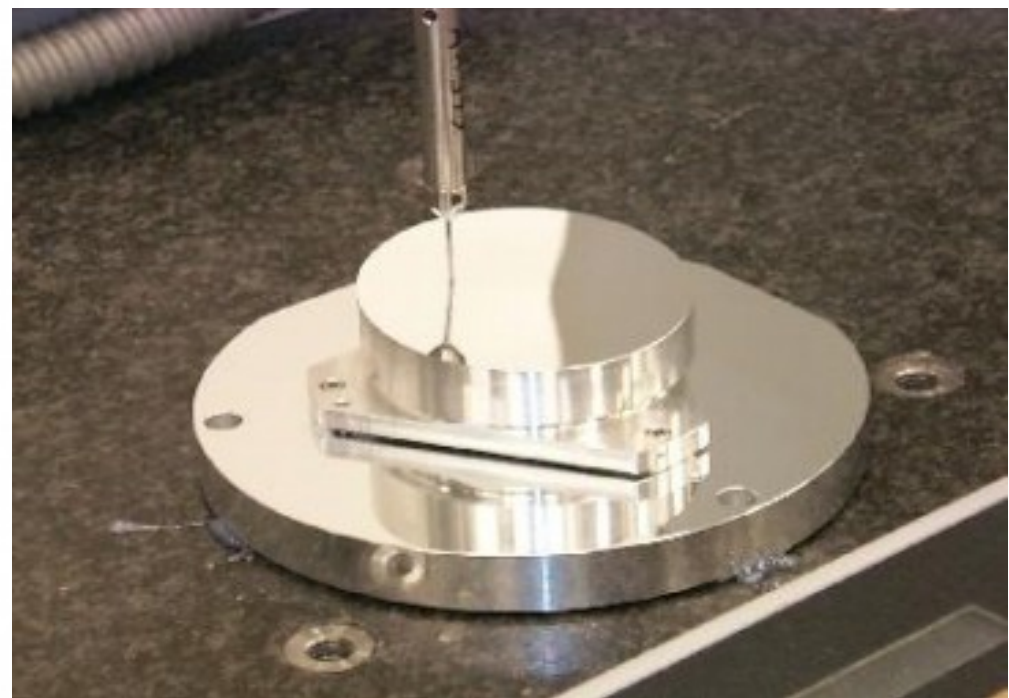
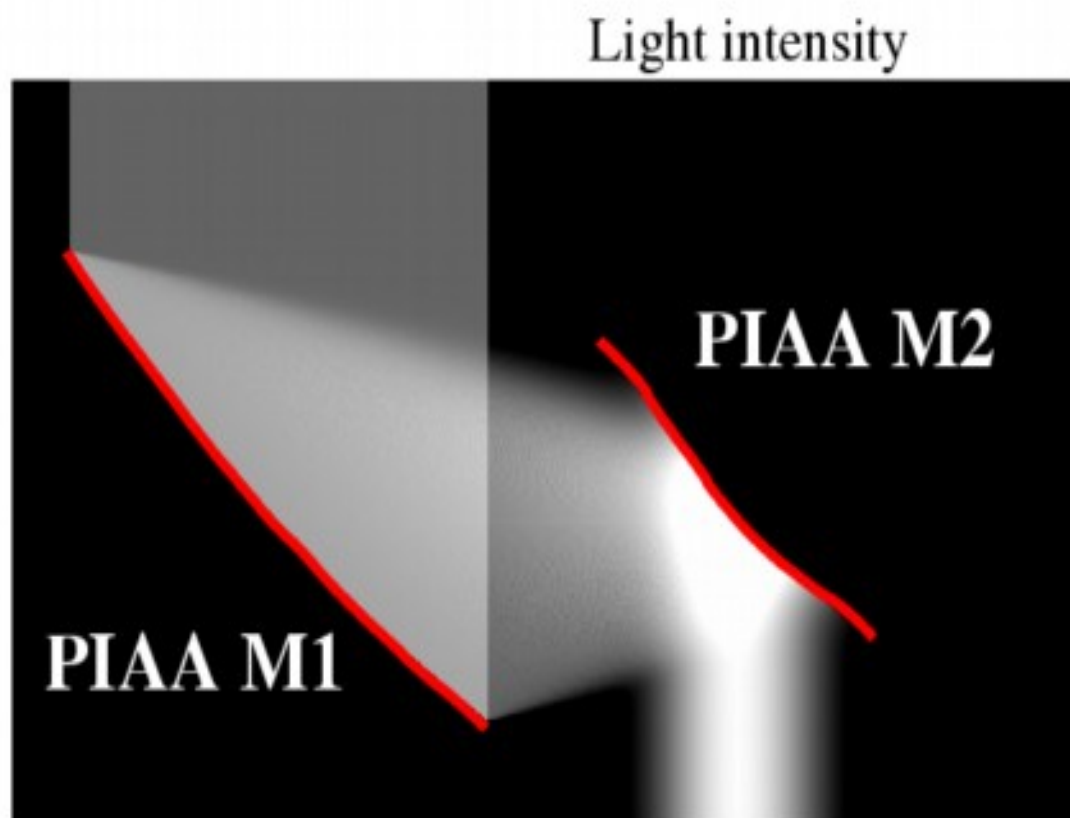


Yang & Kostinski 2004, ApJ, 605, 892
Codona & Angel 2004, ApJ, 604, L117

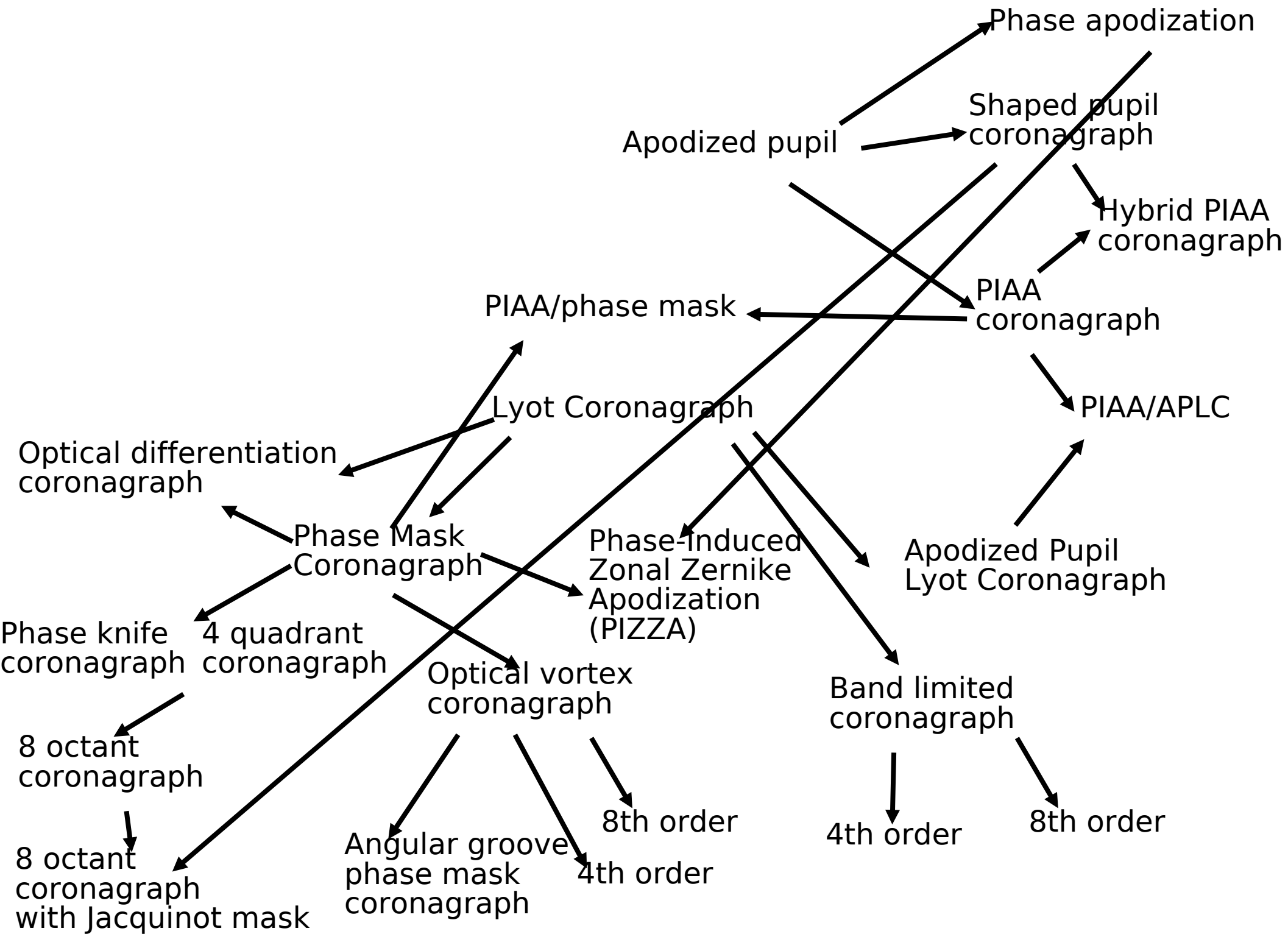
FIG. 9.—Broad-bandwidth light reduction effect on one quadrant of focal plane. The simulation is based on a rectangular spectrum distribution with total bandwidth of $0.6\lambda_0$. (a) $\log_{10}$ relative intensity image when phase $\phi(x, y) = a \tan[0.5 - \epsilon]2\pi x/D + a \tan[0.5 - \epsilon]2\pi y/D$, with $a = 1$ and $\epsilon = 0.005$, is applied to a square pupil. (b) The thicker line represents the $\log_{10}$ relative intensity along the diagonal line crossing the second and the fourth quadrants in (a). The thinner line represents the one without phase modulation. (c) Same as (a), but with phase $\phi(x, y)$ from eq. (11), with $a = 3$ and $\epsilon = 0.001$, applied to a square pupil. (d) Same as (b), but for the quadrants in (c). One can see that the reduction level of 10^{-12} , with an inner working distance of about $3.5\lambda_0/D$, can still be kept with a broad bandwidth of $0.6\lambda_0$ in the second quadrant.

Phase-Induced Amplitude Apodization Coronagraph (PIAAC)

Lossless apodization by aspheric optics.



Guyon, Belikov, Pluzhnik, Vanderbei, Traub, Martinache ... 2003-present



"Interferometric" coronagraphs

= **Nulling interferometer on a single pupil telescope**

- Creates multiple (at least 2) beams from a single telescope beam
- Combines them to produce a destructive interference on-axis and constructive interference off-axis

Achromatic Interferometric Coronagraph Common Path AIC

**AIC
CPAIC**

[Baudoz et al. 2000](#), [Tavrov et al. 2005](#)

Destructive interference between pupil and flipped copy of the pupil
Achromatic PI phase shift and geometrical flip performed by going through focus

Visible Nulling Coronagraph, X & Y shear, 4th order VNC

[Shao et al.](#), [Menesson et al. 2003](#)

Destructive interference between 2 copies of the pupil, sheared by some distance.
4th order null obtained by cascading 2 shear/null

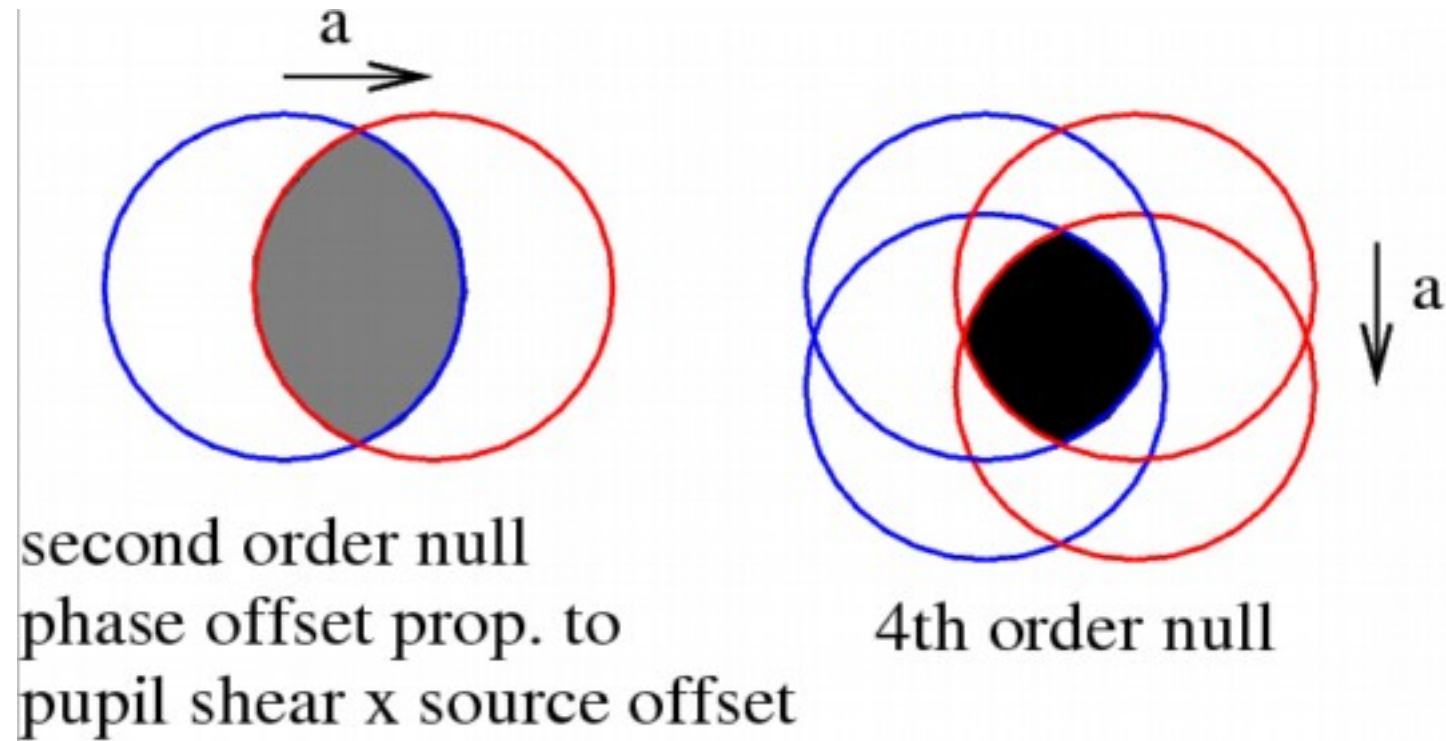
Pupil Swapping Coronagraph

PSC

[Guyon & Shao, 2006](#)

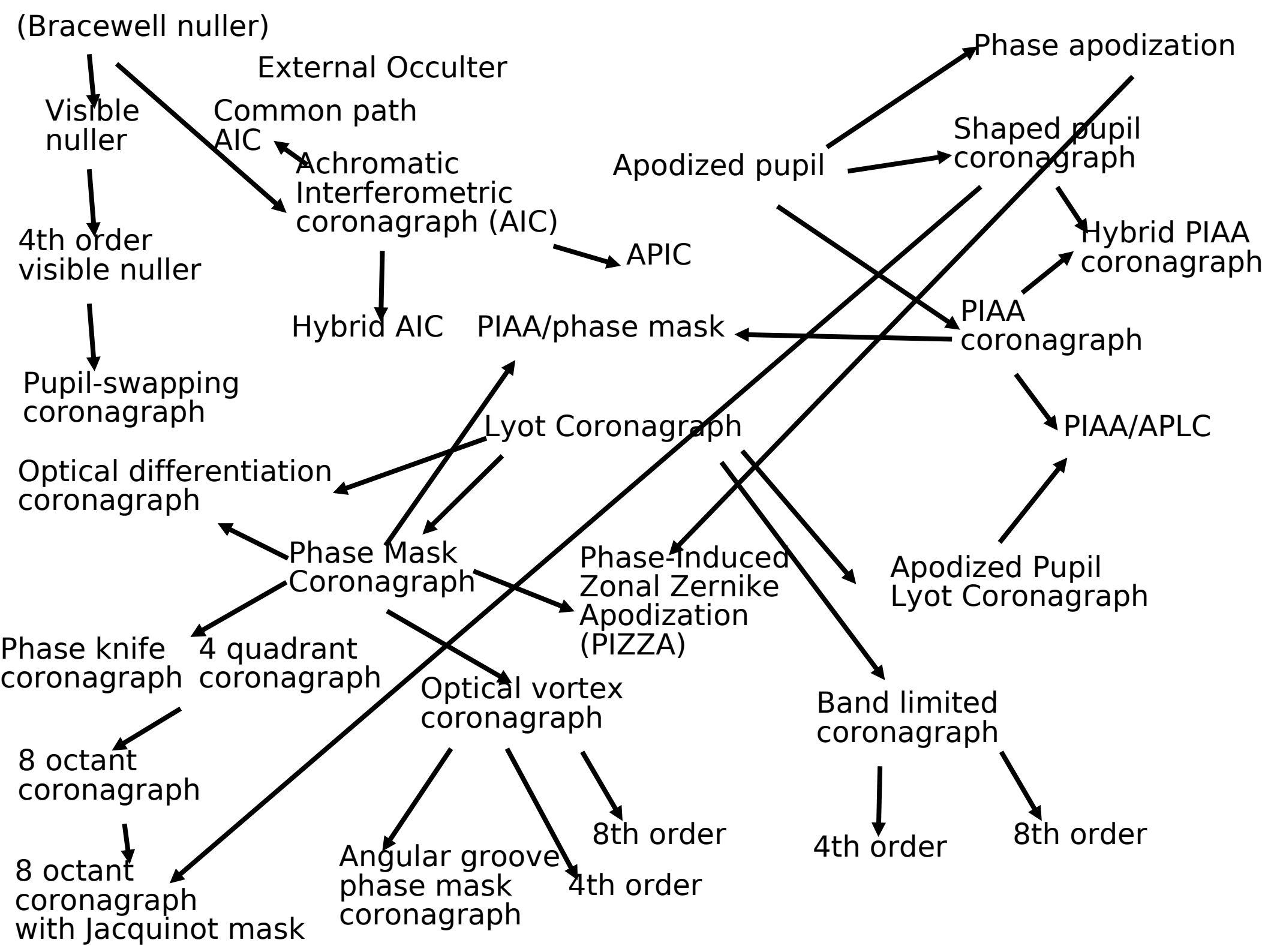
Destructive interference between pupil and a copy of the pupil where 4 quadrants have been swapped

Visible Nuller Coron. (VNC)

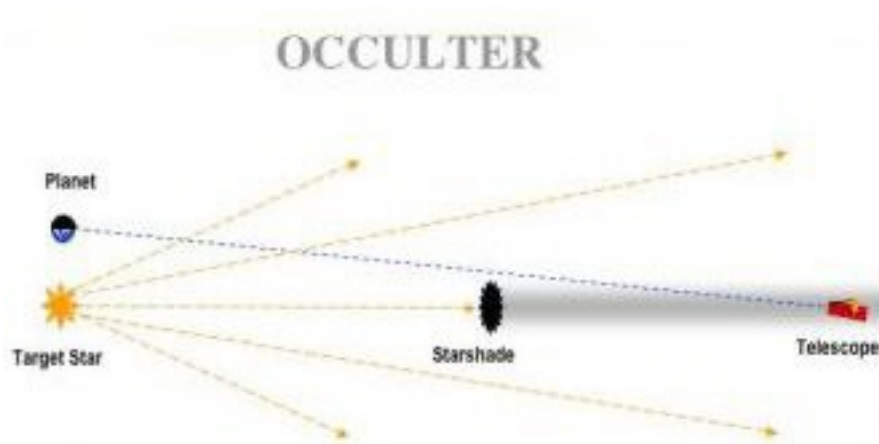


Small shear : high throughput, low IWA
Large shear : low throughput, small IWA
The 2 shears can also be colinear

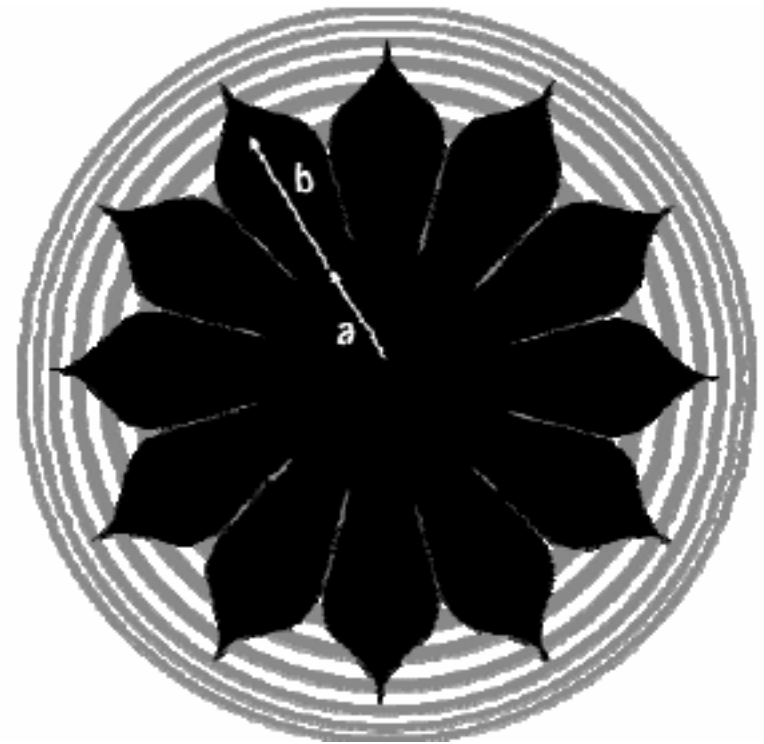
**Sounding rocket
(PICTURE)**

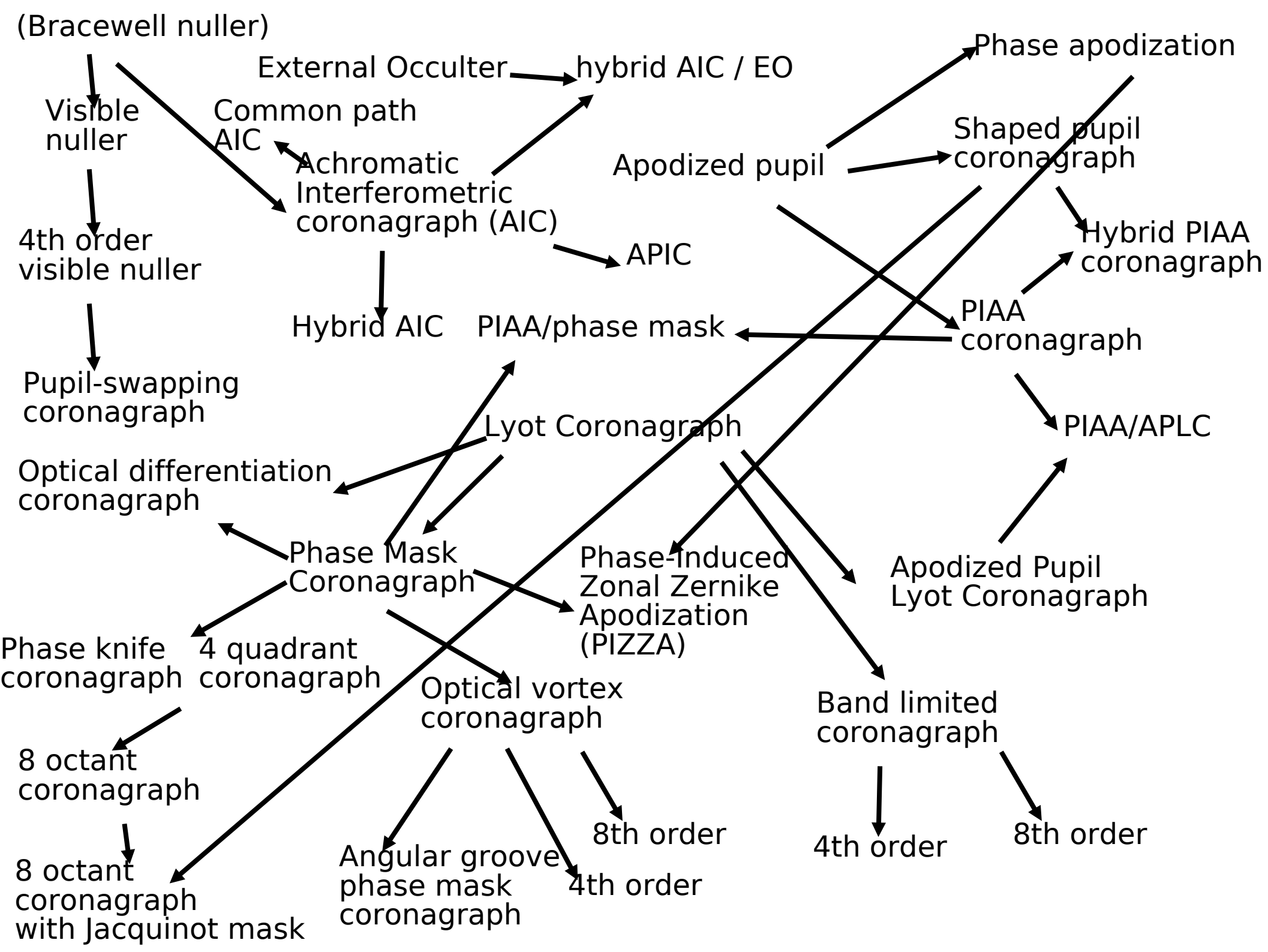


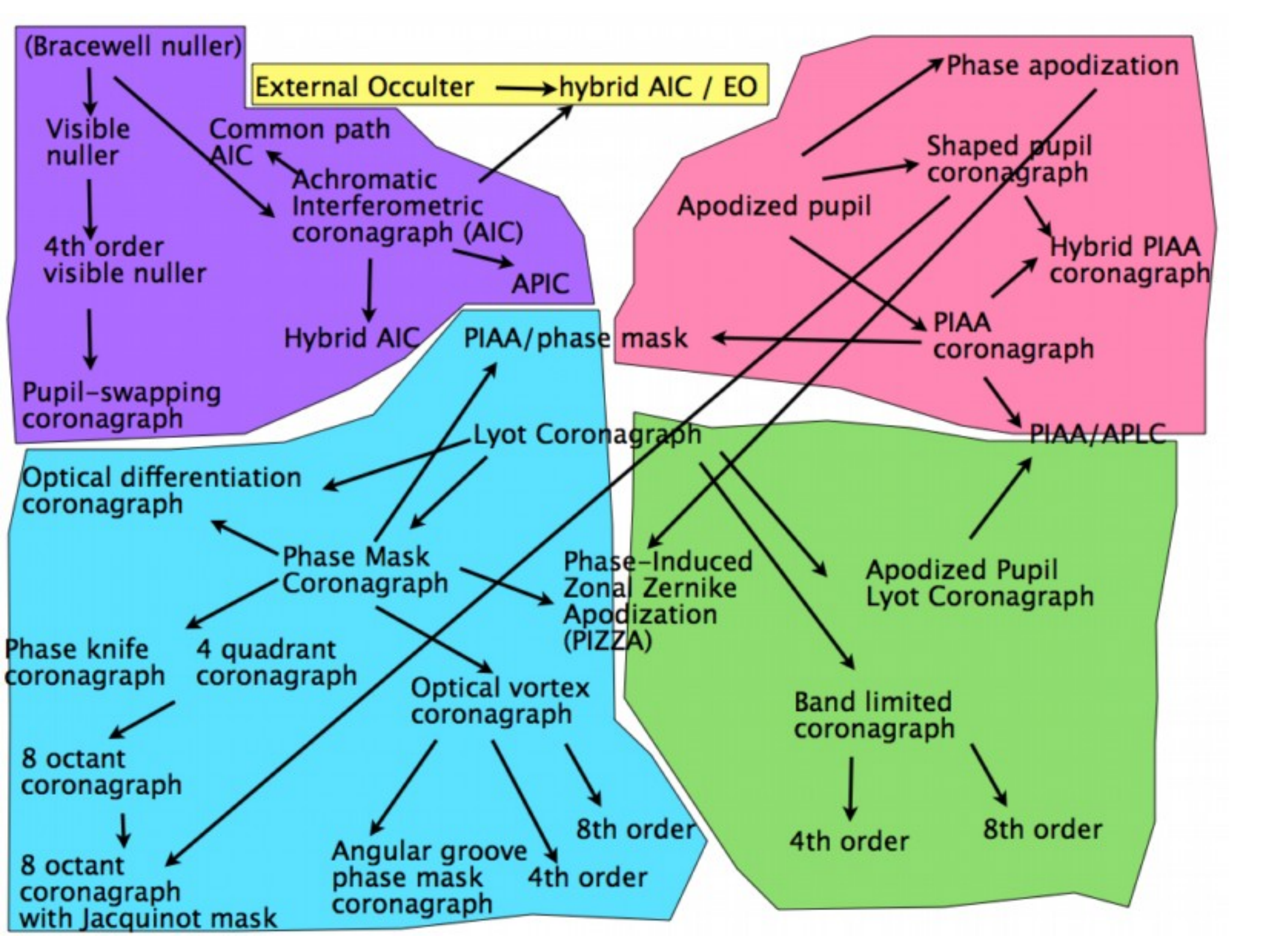
External Occulter



A properly placed and shaped occulter can drop a deep shadow of starlight over a telescope while allowing planet light to pass unimpeded.







Coronagraph systems

What is a high contrast imaging system (ground or space) ?

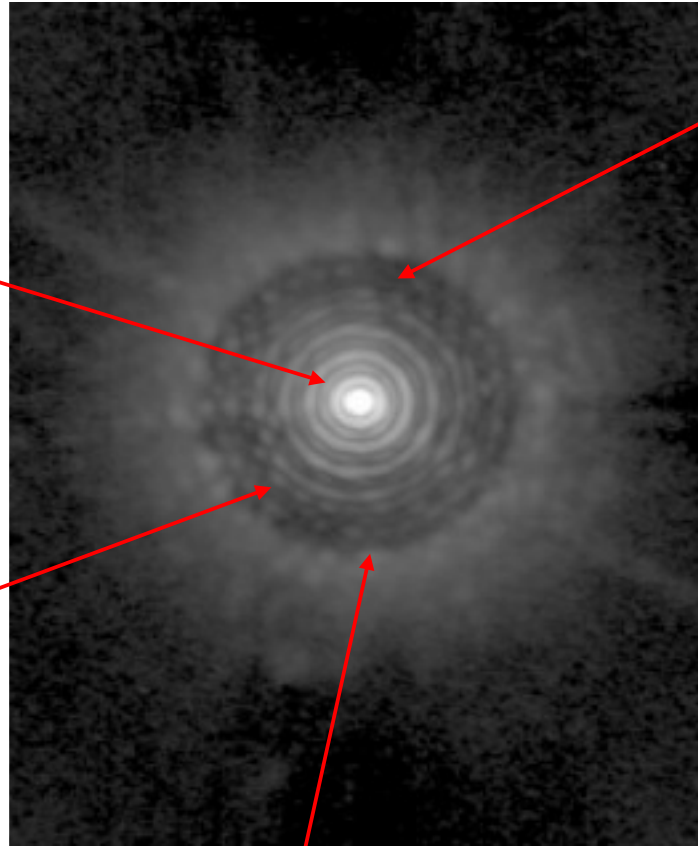
Imaging system optimized to provide high contrast at small angular separation.

Key elements:

- **Coronagraph** or nulling interferometer to optically remove starlight and isolate planet light (overcomes diffraction)
- **Wavefront correction system** to reduce and calibrate residual wavefront errors
 - For coronagraphs: Extreme-AO system to flatten wavefront
 - For interferometers: Optical pathlength sensing / correction (+ AO on individual apertures of the interferometer)
- **Science detector (+ differential detection technique)** for imaging, spectroscopy and polarimetry
 - (note: the science detector can be part of the wavefront control system, and measure residual scattered light to be removed)

From conventional AO to Coronagraphic Extreme-AO

We use a non-extreme AO system image as starting point
Example of a very good PSF with a current AO system: LBT AO image



PSF diffraction
(Airy rings, spiders)

**REMOVED BY
CORONAGRAPH**

Static and slow
speckles

**MUST BE
REMOVED BY
CALIBRATION SYSTEM
OR DIFFERENTIAL IMAGING
(actively or in post
processing)**

Residual atmospheric
speckle halo

**REDUCED BY FAST,
ACCURATE AND
EFFICIENT AO SYSTEM**

Control radius of AO
**DEFINED BY NUMBER
OF ACTUATORS IN DM:
MAY BE INCREASED WITH
MORE ACTUATORS IF REQUIRED**

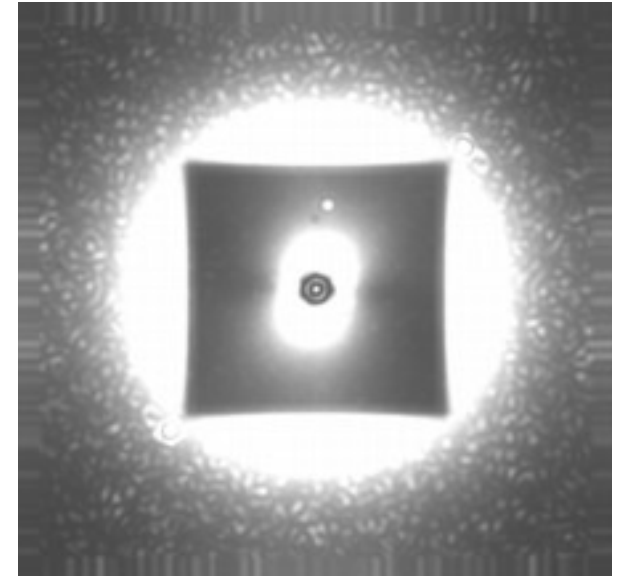
Wavefront control for High contrast imaging

Ground-based systems

Residual speckle field is brighter than planets(s)

Systems often operate in **speckle noise limited regime**

→ calibrating speckles is extremely important



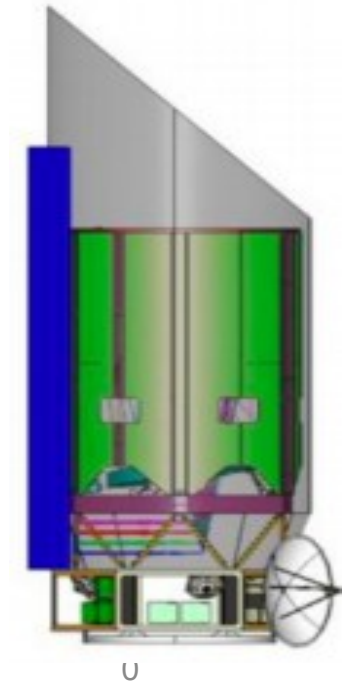
Space-based ultra-high contrast systems

Detection is close to the **photon noise limit** of the planet(s)

→ speckles need to be reduced at or below the planet image surface brightness level

Wavefront control is essential, and differential imaging/calibration will not work if speckle halo is brighter than planet

→ need to build extremely stable system



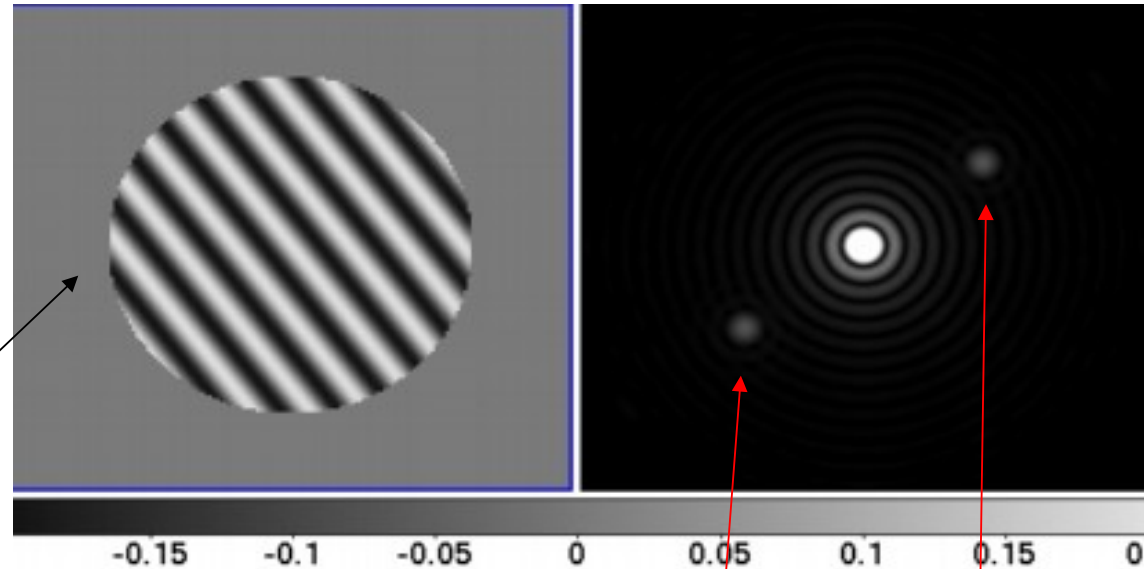
Relationship between speckle and wavefront errors

pupil plane complex amplitude

$$W(\vec{u}) = \mathcal{A}(\vec{u}) e^{i\phi(\vec{u})}$$

Cosine aberration in pupil phase

$$\phi(\vec{u}) = \frac{2\pi h}{\lambda} \cos(2\pi \vec{f} \vec{u} + \theta)$$



$$I(\vec{\alpha}) = PSF(\vec{\alpha}) + \left(\frac{\pi h}{\lambda}\right)^2 [PSF(\vec{\alpha} + \vec{f}\lambda) + PSF(\vec{\alpha} - \vec{f}\lambda)]$$

EXAMPLE:

Earth-like planet around Sun-like star is $\sim 1e-10$ contrast

In visible light, $h = 1.6e-12$ m (0.0012 nm) = $1e-10$ speckle

$1e-10$ speckle (or $1e-10$ contrast planet) around Sun at 10pc = 0.1 ph/sec/m²/um

On a 4-m telescope, with 10% efficiency and a 0.5 um spectral band:

Earth = 0.6 ph/sec

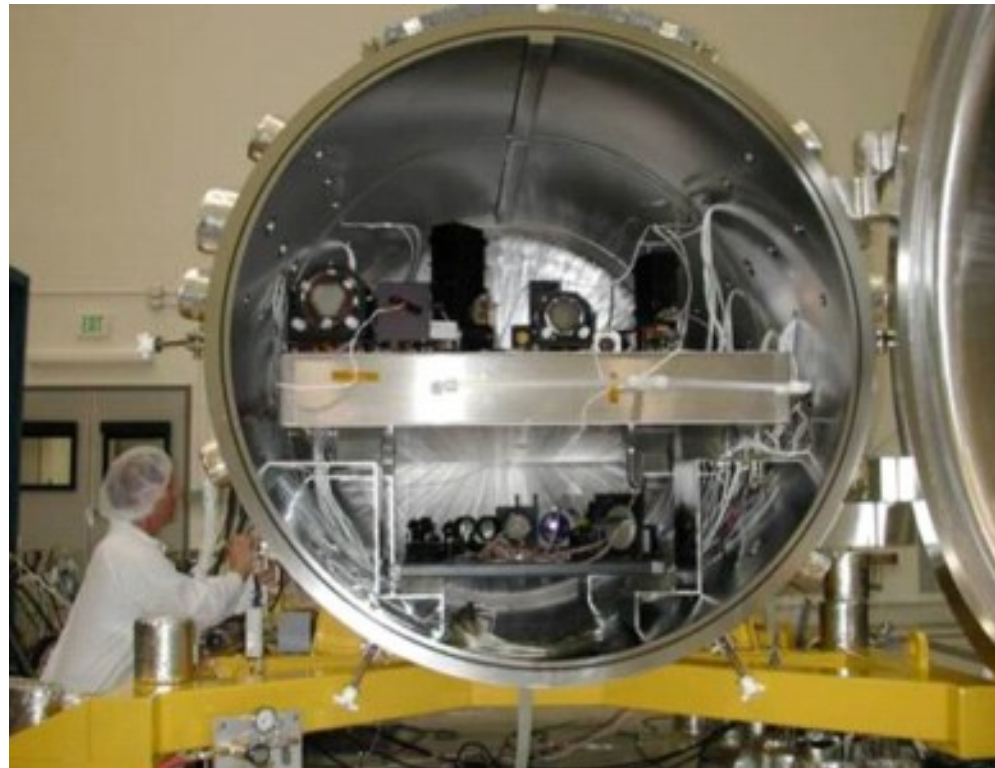
To measure phase and amplitude of speckle requires ~ 10 photon

10 photon = 16 sec

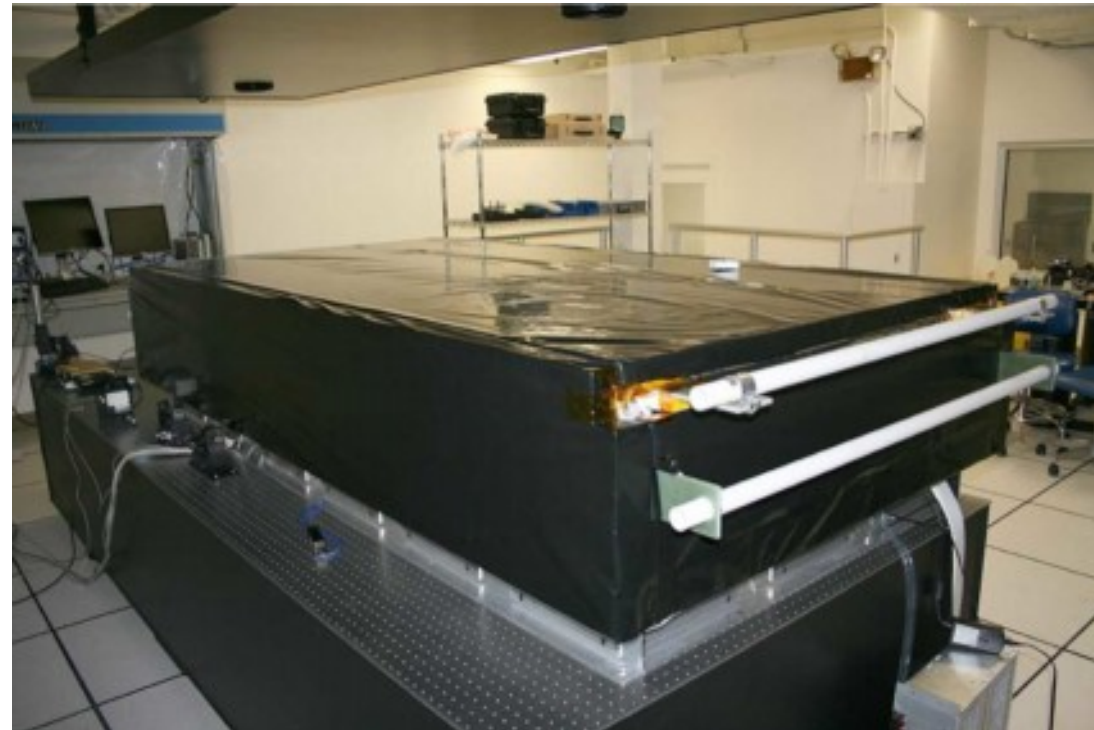
→ **This spatial frequency needs to be stable to 1/1000 nm over ₃ ~ minute**

Coronagraphy testbeds for high contrast ($< 1e-8$) work need to achieve high stability

*High Contrast Imaging Testbed (HCIT) is a
vacuum facility at NASA JPL*

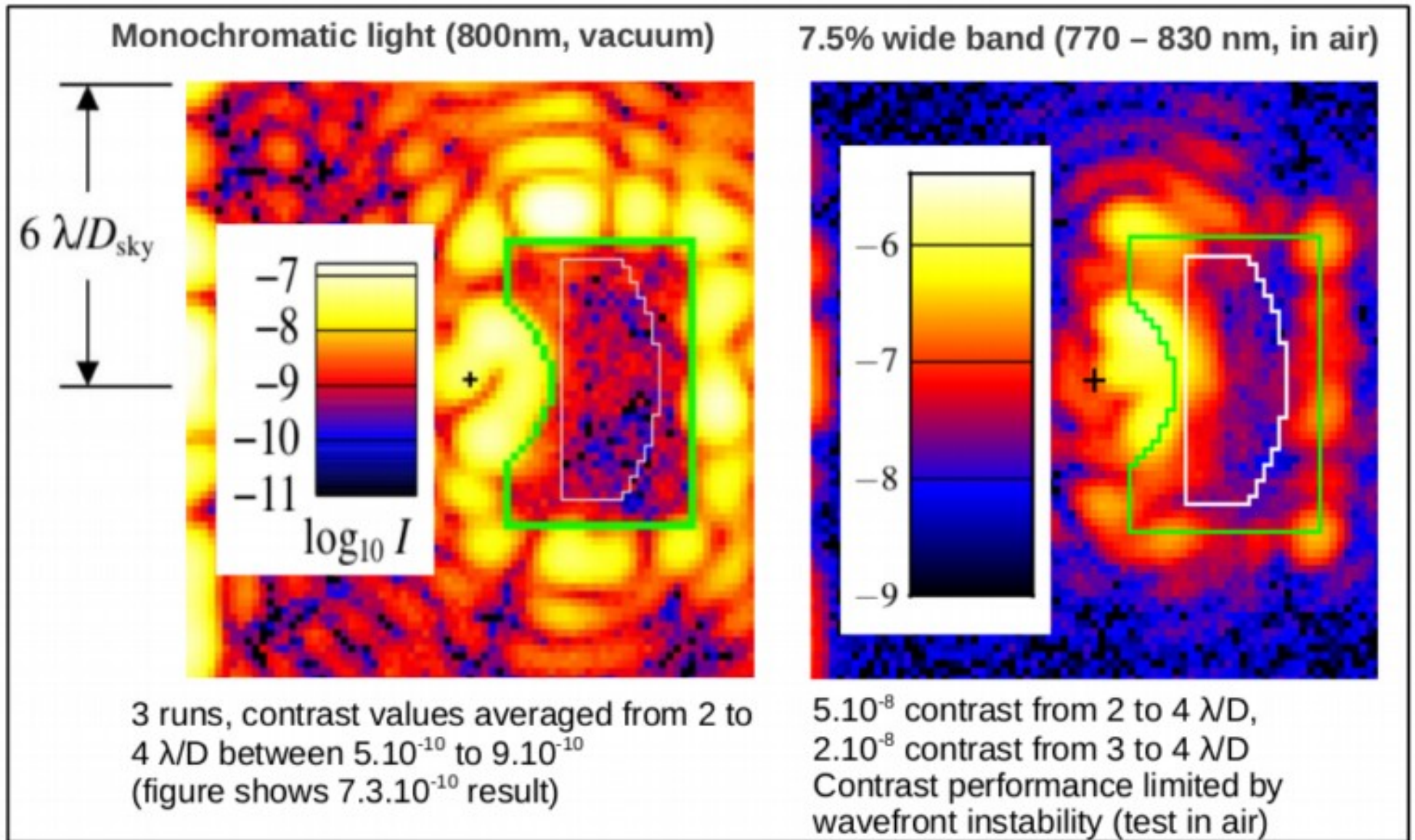


*NASA Ames testing PIAA coronagraph /
WFC architectures & MEMs DMs.*



High contrast images obtained in NASA labs

Example: PIAA coronagraph lab results



Current and future high contrast systems - ground

NICI on Gemini South telescope - ongoing, large survey completed

85-element curvature AO system + Lyot coronagraph

Differential imaging capability (methane absorption line)

HiCIAO on Subaru Telescope - ongoing survey

188-element curvature AO system + Lyot coronagraph

Differential imaging capability (methane absorption line)

→ **Subaru Coronagraphic Extreme AO (upgrade of HiCIAO)** - on sky since 2012

Small inner working angle PIAA coronagraph

Pointing sensing and control with coronagraphic low order WFS

Speckle control using focal plane image as sensor

32x32 MEMS deformable mirror (upgraded 2013 to 2000 elements)

Includes Integral Field Spectrograph to help remove speckles and acquire spectra

P1640 + Palm300 on Palomar 5-m telescope - on sky since 2012

3000 element high order AO system + Lyot coronagraph

Includes Integral Field Spectrograph to help remove speckles and acquire spectra

Gemini Planet Imager (GPI) - large survey will start observations in late 2013

ExAO system using 64x64 MEMS DM + coronagraph

Includes calibration interferometer to accurately measure residual speckles

Includes Integral Field Spectrograph to help remove speckles and acquire spectra

ESO's SPHERE on VLT - large survey will start observations in late 2013

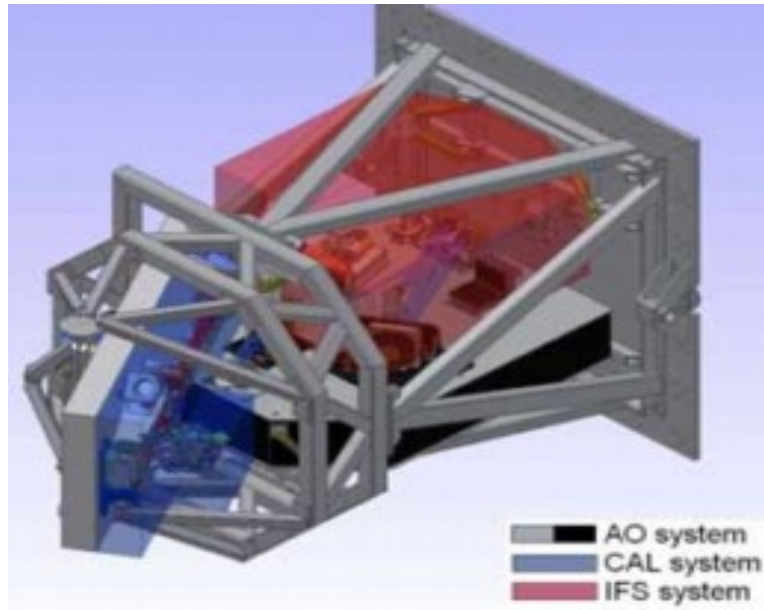
ExAO system + coronagraph

Highly stable bench

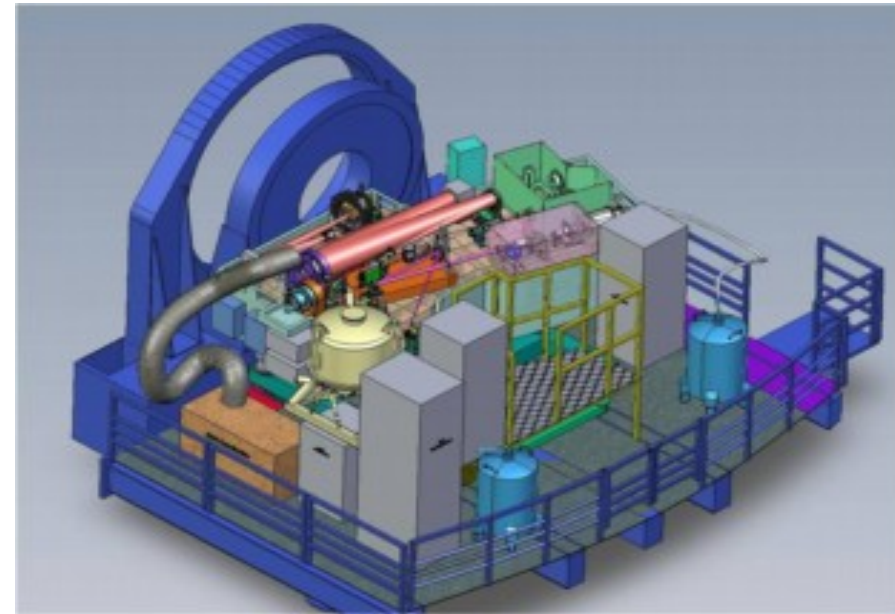
Includes Integral Field Spectrograph to help remove speckles and acquire spectra

Includes differential polarimetric imager

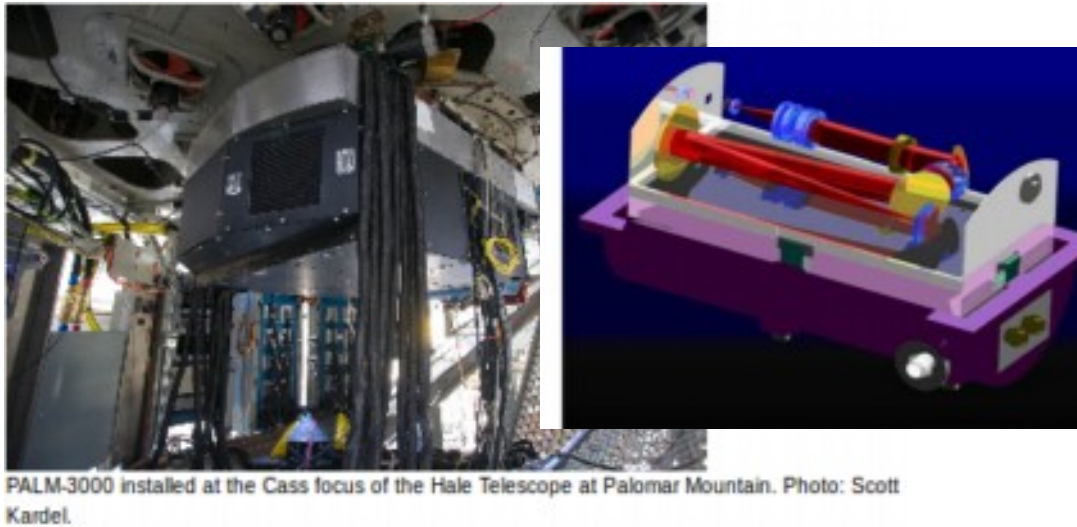
Current and future high contrast systems - ground



Gemini Planet Imager

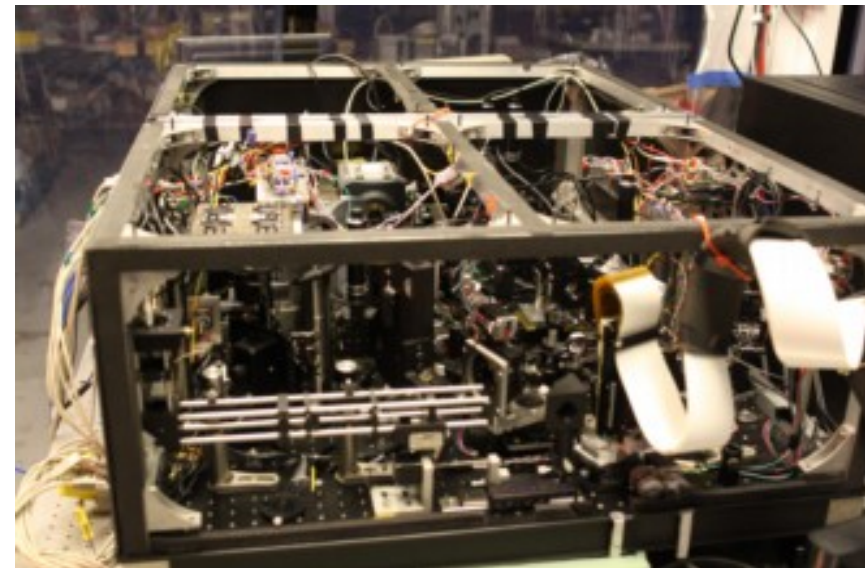


SPHERE (European Southern Observatory)



PALM-3000 installed at the Cass focus of the Hale Telescope at Palomar Mountain. Photo: Scott Kardel.

PALM3000/P1640 (Palomar 5-m Telescope)



Subaru Coronagraphic Extreme-AO