

# An Evidence of Dark Matter Accumulation at Sgr A\* from S0-2 Star Observational Data

**SAIDA Hiromi** (Daido Univ.) / 齊田浩見 (talk)

**UCHIDA Shun-ya** (Naogya Univ.) / 内田舜也

**NISHIYAMA Shogo** (Miyagi U. Edu.) / 西山正吾

+ Members in Subaru Proposal/Kakenhi Grants/Bayesian Team

- Subaru Users Meeting 2026FY (NAOJ, Mitaka) 2026/06/17 - 19
- Traversing the Galactic Center in Space and Time 2026/05/18 - 22  
(Brno Planetarium & Observatory. Czech)
- Subaru Users Meeting 2025FY (NAOJ, Mitaka) 2025/10/29 - 31

Authors of this report/paper (in preparation)

UCHIDA Shun-ya (Nagoya U.) / 内田舜也 名古屋大学

SAIDA Hiromi (Daido U.) / 斉田浩見 大同大学

MATSUI Sena (Nagoya U.) / 松井瀬奈 名古屋大学

TAKEUCHI T. Tsutomu (Nagoya U.) / 竹内努 名古屋大学

NISHIYAMA Shogo (Miyagi U. of Edu.) / 西山正吾 宮城教育大学

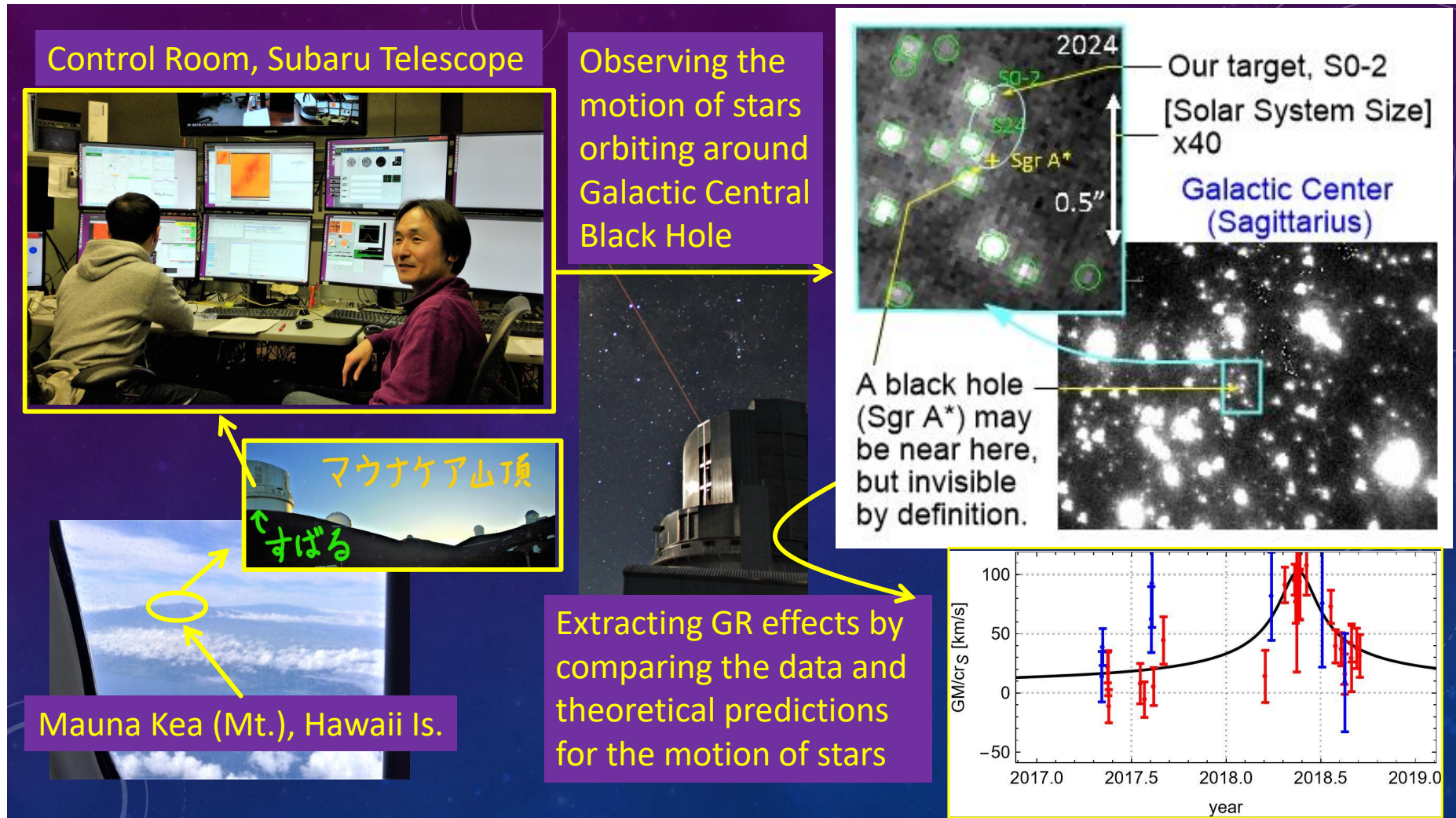
TAKAMORI Yohsuke (Wakayama NITC) / 孝森洋介 和歌山高専

TAKAHASHI Masaaki (Aichi U. of Edu.) / 高橋真聡 愛知教育大学

# 1. Sgr A\* and GR

GR = General Relativity

- Subaru GC research **beyond GR** is launched



- $S0-2$  is a little bit bright and near to  $Sgr A^*$ ,  
enough to detect GR effect with AO.
- Fact  
Rejection of Newton Gravity compared to  
General Relativistic Black Hole in vacuum  
(GRAVITY collab. A&A 2018 ; Do et al. 2019 Science ; Saida et al. 2019 PASJ)
- Note
  - ◇ Some “modified gravity theories” are alive  
for some issues:  
Cosmic censorship, Global hyperbolicity,  
Dark matter, Dark energy,  $H_0/S_8$  tension, and so on.
  - ◇ Environment of  $Sgr A^*$  is not exactly vacuum.

- Our aims/key questions

Is a Modified Gravity Theory favored?

Is Dark Matter accumulating at Sgr A\*?

→ Method (explained from the next page)

Parametrized Post-Newtonian (PPN) formalism

[Saida et al. 2024 Prog.Theor.Exp.Phys](#) (talk in last year)

- Other aim: Origin of stars in GC

→ Poster by S.Nishiyama

[Nshiyama et al. 2024 Proc.Jpn.Acad.](#) & [2025 Universe](#)

# 2. Theoretical Framework

## 2.1 Taylor expansion of grav. field

- Post-Newtonian (PN) parameter ( $V_p \simeq 0.03c$ )

$$\varepsilon_p \sim \frac{GM_{\text{BH}}}{c^2 r_p} \approx \left(\frac{V_p}{c}\right)^2 \sim 10^{-3} \in \boxed{\text{Un-explored region in } (M_{\text{BH}}, \varepsilon) \text{ space}}$$

- PN expansion: Taylor expansion of Grav. Pot. of Kerr BH (BH in GR)  $g_{\mu\nu}^{\text{Kerr}}$  by  $\varepsilon$
- **Parametrized PN formalism** : Introduce some artificial parameters in the PN expansion of  $g_{\mu\nu}^{\text{Kerr}}$

## 2.2 PPN expansion and parameters

- BH's metric tensor / stationary axialsymmetric

$$g_{tt} = -1 + 2\varepsilon(r) + \mathbf{A} \varepsilon(r)^2 + O(\varepsilon^3) \quad , \quad m = GM_{\text{BH}}/c^2$$

$$g_{tx} = +2q \frac{x}{r} \varepsilon(r)^2 + O(\varepsilon^3) \quad , \quad q = \frac{cJ_{\text{BH}}}{GM_{\text{BH}}^2} \quad \boxed{\varepsilon(r) = \frac{m}{r}}$$

$$g_{ty} = -2q \frac{y}{r} \varepsilon(r)^2 + O(\varepsilon^3)$$

$$g_{tz} = +2q \mathbf{C}_z \frac{z}{r} \varepsilon(r)^2 + O(\varepsilon^3)$$

$$g_{ij} = \delta_{ij} + 2\mathbf{B} \frac{x^i x^j}{r^2} \varepsilon(r) + O(\varepsilon^2)$$

The simplest PPN form with  $A$ ,  $B$ ,  $C_z$  for measuring deviation from GR.

- Kerr (GR BH in vac.) case  $\Rightarrow$   $\boxed{A = C_z = 0, B = 1}$

## 2.3 Science targets with Subaru/TMT

- One science target with Subaru

$A$  and  $B$  are the effects of Sgr  $A^*$  mass  $M_{\text{BH}}$

→  $A, B$  are 1PN order, in Dec., R.A. and  $z$

- One science target with TMT (Thirty-Meter-Telescope)

$C_z$  is the effects of Sgr  $A^*$  spin  $J_{\text{BH}}$

→  $C_z$  is 1.5PN order, not detectable with Subaru.

- Currently we consider  $A$  and  $B$  without  $C_z$ .

- Important note for  $A$  and  $B$  ...

- Important note for  $A$  and  $B$ :

If  $|A| > O(10)$  and/or  $|B| > O(10)$ ,

then the **gravitational lens** effect (due to BH mass) becomes **detectable** with Subaru.

### Difference from other groups

In our PPN model, **the grav. lens effect is included**, while the grav. lens effect has not been considered in reports by Keck and VLT/GRAVITY groups.

# 3. Bayesian fitting

- Search the value of 19 + 2PPN parameters:
  - theoretical prediction of S0-2's motion  
in the PPN form of grav. pot.
  - fitting the theoretical prediction  
with Obs. Data of S0-2's motion
- 19 parameters, except for  $\{A, B\}$  are  $\dots$

- 19 parameters, except for  $\{A, B\}$

$M_{\text{BH}}$  : Mass of Sgr A\* (massive BH)

$R_{\text{GC}}$  : Distance to Sgr A\* (Galactic Center)

$(\vec{a}_{\text{BH}})$  : BH spin (magnitude and direction)  $\leq 1.5\text{PN}$

$\vec{x}_{\text{apo}}, \vec{v}_{\text{apo}}$  : S0-2's initial conditions (6 components)

$\vec{V}_{\text{obs}}$  : Our velocity w.r.t. Sgr A\* (3 comp.)

$(X, Y)_{\text{Keck}}$  : Astro. reference point for Keck

$(\dot{X}, \dot{Y})_{\text{Keck}}$  : Velocity of the ref. point for Keck

$(X, Y)_{\text{VLT}}$  : Astro. reference point for VLT

$(\dot{X}, \dot{Y})_{\text{VLT}}$  : Velocity of the ref. point for VLT

$(X, Y) = (\text{R.A.}, \text{Dec.})$

NOTE:  $\left\{ \begin{array}{l} \text{Our coordinate origin is at Sgr A*} \\ \text{Assume } \vec{v}_{\text{E}} \text{ and } (\dot{X}, \dot{Y}) \text{ are constant} \end{array} \right.$

- Data set used in this report:  $\simeq 500$  data points
  - VLT's open data, 1992–2016
  - Keck's open data, 1995–2018
  - Our Subaru data, 2014–2018

Subaru Data taken with NIR-Wave Front Sensor + AO3k

◇ have been used for “origin of stars at GC”.

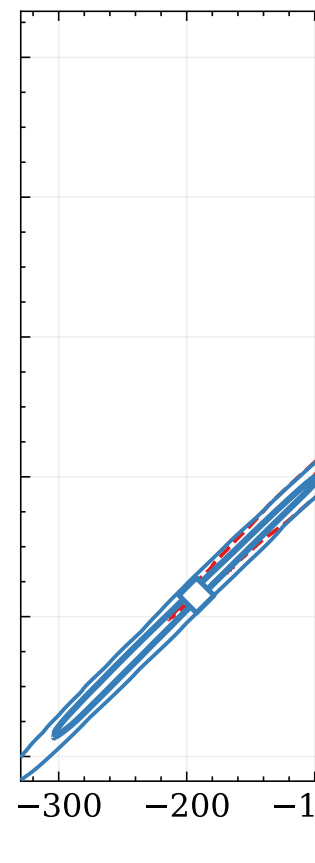
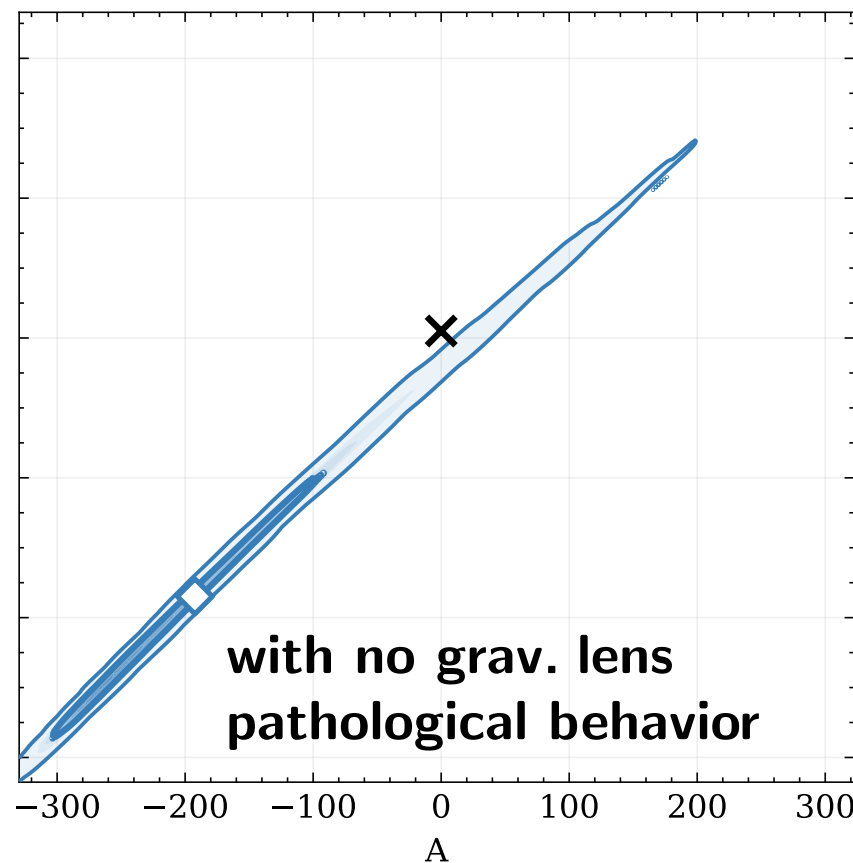
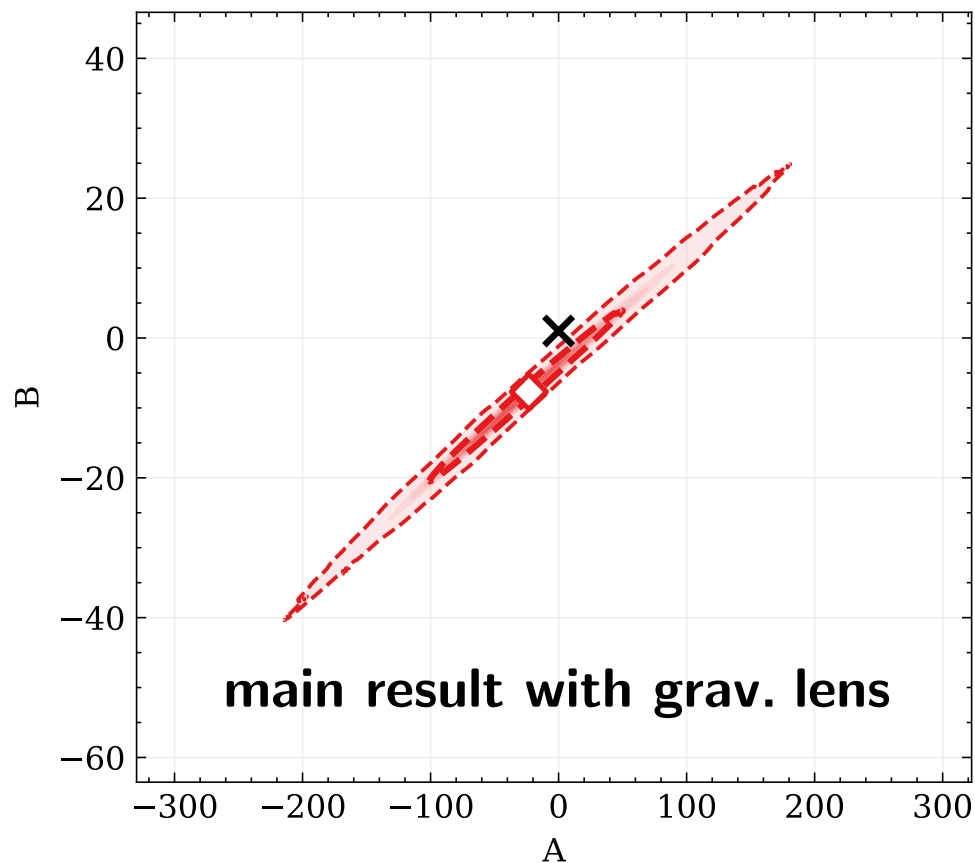
→ see poster by Shogo Nishiyam

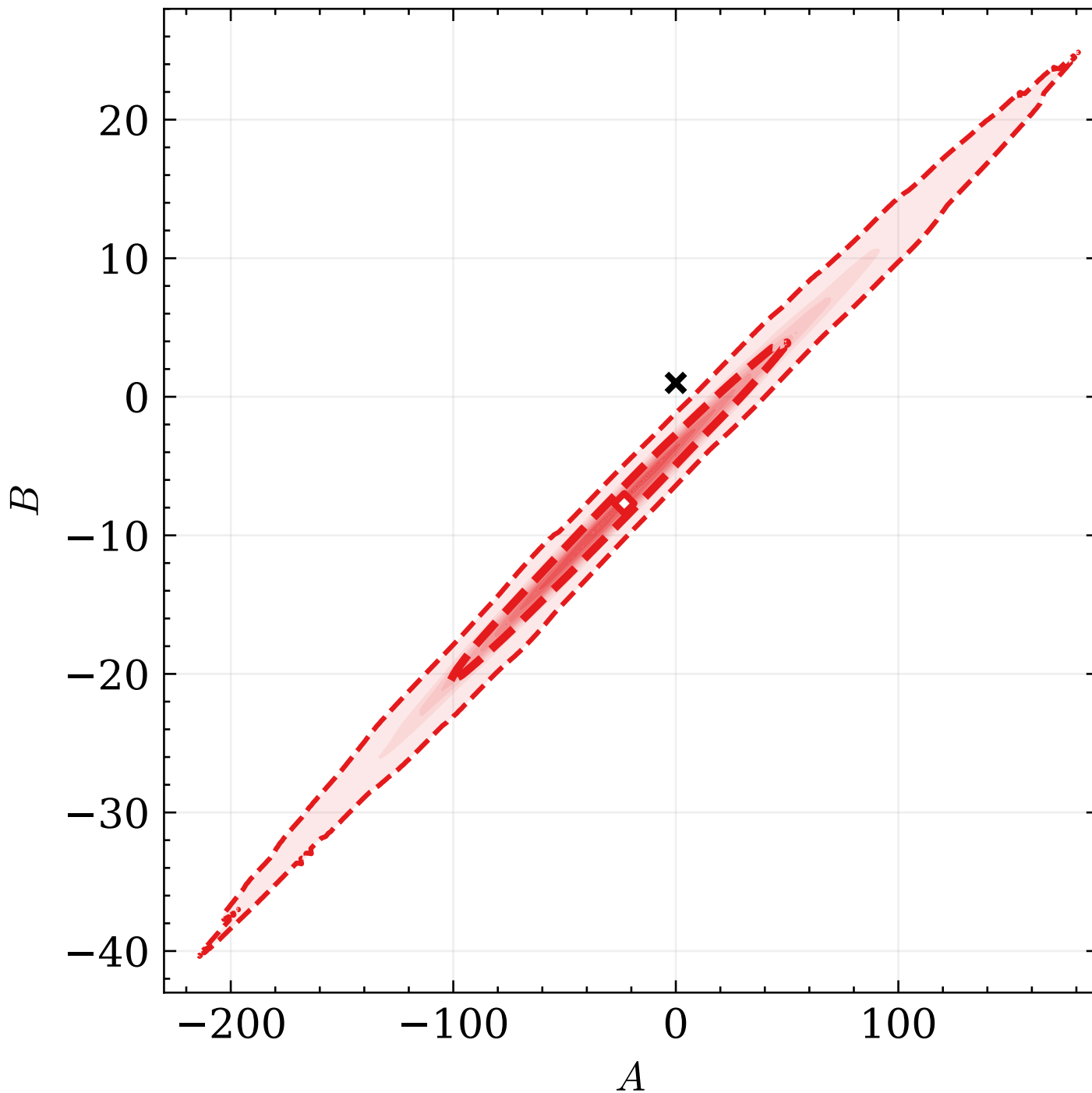
◇ are left to be analyzed for S0-2's motion.

You are welcome, having interests in analyzing those data!

- We are doing Bayesian-fitting — **Preliminary**  
with flat prior probability distribution
- ◇ Posterior probab. distr. of the PPN para.  $(A, B)$

- - - with 1PM   
 — without 1PM   
 — 68% Highest Posterior Density (HPD)   
 — 99.9% HPD   
 ✕ Schwarzschild (0,1)   
 ◇





**Preliminary**

GR BH in vac.  
is excluded from  
99.9% region of  
Highest  
Posterior  
Density

# ◇ Preliminary result of all parameter values

Parameter		Median, central 68%	HPD 68% interval
$M_{\text{BH}}$	$[10^6 M_{\odot}]$	$4.009^{+0.042}_{-0.041}$	[3.969, 4.052]
$A$		$-24.9^{+51.8}_{-48.1}$	[-77.5, 22.0]
$B$		$-7.9^{+8.4}_{-8.0}$	[-16.0, 0.4]
$R_{\text{GC}}$	[kpc]	$7.9865^{+0.0411}_{-0.0409}$	[7.944, 8.026]
$V_{\text{obs}}^{\text{X}}$	[arcsec yr <sup>-1</sup> ]	$(-0.18^{+6.75}_{-6.77}) \times 10^{-3}$	$[-4.5, 9.0] \times 10^{-3}$
$V_{\text{obs}}^{\text{Y}}$	[arcsec yr <sup>-1</sup> ]	$(-0.03^{+6.96}_{-6.82}) \times 10^{-3}$	$[-3.8, 9.9] \times 10^{-3}$
$V_{\text{obs}}^{\text{Z}}$	[km s <sup>-1</sup> ]	$-10.30^{+2.57}_{-2.44}$	[-12.89, -7.89]
$\text{Dec}_{\text{Keck}}$	[arcsec]	$(-1.442^{+0.221}_{-0.223}) \times 10^{-3}$	$[-1.658, -1.215] \times 10^{-3}$
$\text{RA}_{\text{Keck}}$	[arcsec]	$(9.15^{+1.28}_{-1.33}) \times 10^{-4}$	$[7.89, 10.49] \times 10^{-4}$
$V_{\text{Keck}}^{\text{Dec}}$	[arcsec yr <sup>-1</sup> ]	$(-0.05^{+6.77}_{-6.76}) \times 10^{-3}$	$[-9.2, 4.2] \times 10^{-3}$
$V_{\text{Keck}}^{\text{Ra}}$	[arcsec yr <sup>-1</sup> ]	$(-0.10^{+6.82}_{-6.95}) \times 10^{-3}$	$[-9.9, 3.7] \times 10^{-3}$
$\text{Dec}_{\text{VLT}}$	[arcsec]	$(1.21^{+2.27}_{-2.29}) \times 10^{-4}$	$[-0.96, 3.59] \times 10^{-4}$
$\text{RA}_{\text{VLT}}$	[arcsec]	$(-7.42^{+1.25}_{-1.32}) \times 10^{-4}$	$[-8.66, -6.10] \times 10^{-4}$
$V_{\text{VLT}}^{\text{Dec}}$	[arcsec yr <sup>-1</sup> ]	$(-0.01^{+6.76}_{-6.77}) \times 10^{-3}$	$[-9.2, 4.3] \times 10^{-3}$
$V_{\text{VLT}}^{\text{Ra}}$	[arcsec yr <sup>-1</sup> ]	$(-0.11^{+6.82}_{-6.95}) \times 10^{-3}$	$[-10.0, 3.7] \times 10^{-3}$
$t_{\text{apo}}$	[yr (AD)]	$2010.3346^{+0.0008}_{-0.0008}$	[2010.3338, 2010.3353]
$I_{\text{star}}$	[deg]	$133.869^{+0.147}_{-0.146}$	[133.719, 134.012]
$\Omega_{\text{star}}$	[deg]	$227.684^{+0.128}_{-0.121}$	[227.563, 227.813]
$\omega_{\text{star}}$	[deg]	$66.272^{+0.112}_{-0.107}$	[66.159, 66.376]
$e_{\text{star}}$		$0.88519^{+0.00083}_{-0.00080}$	[0.88441, 0.88603]
$T_{\text{star}}$	[yr]	$16.0501^{+0.0069}_{-0.0065}$	[16.0432, 16.0566]

◇ Pick up some parameters — **Preliminary**

○ Median & 68% Highest Posterior Density:

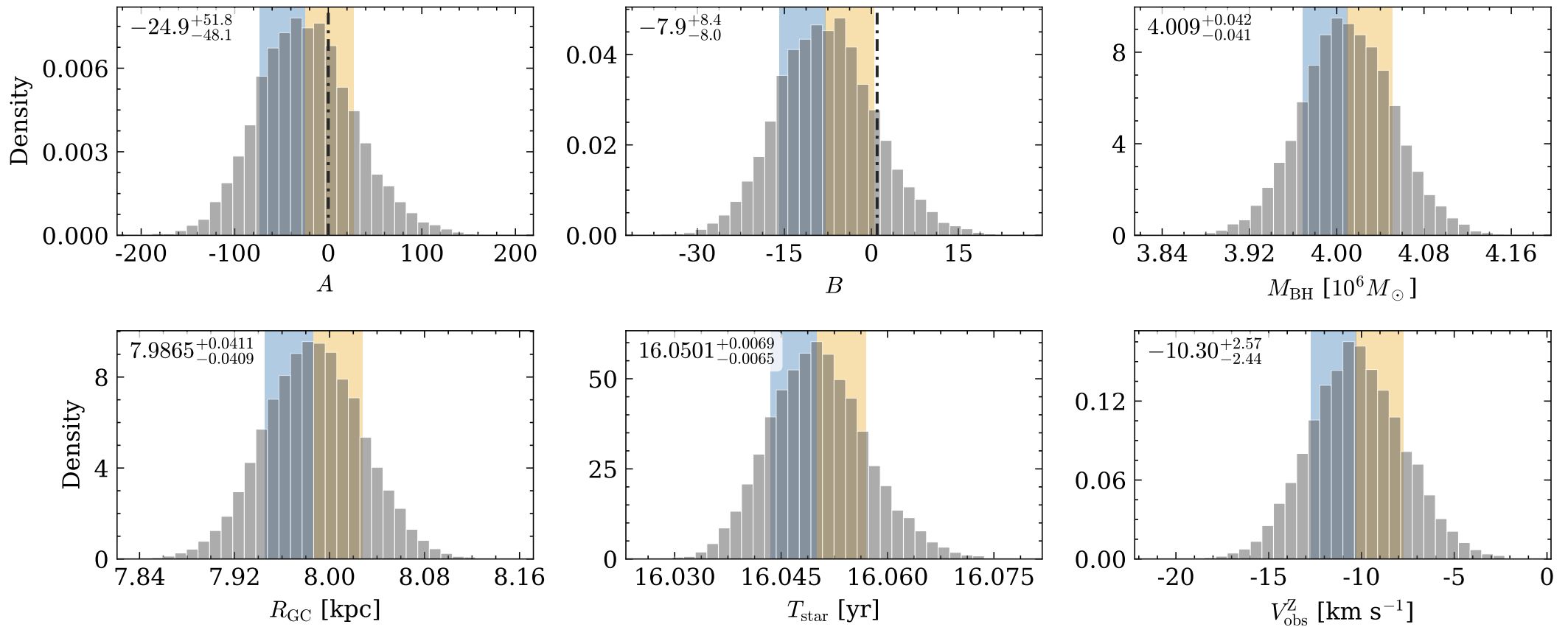
$M_{\text{BH}} [10^6 M_{\odot}]$	:	4.009	+0.0042/	− 0.041
$R_{\text{GC}} [\text{kpc}]$	:	7.9865	+0.0411/	− 0.0409
$T_{\text{star}} [\text{yr}]$	:	16.0501	+0.0069/	− 0.0065
$V_{\text{obs}}^Z [\text{km/s}]$	:	−10.3	+2.57/	− 2.44
$A$ [no.dim.]	:	−24.9	+51.8/	− 48.1
$B$ [no.dim.]	:	−7.9	+8.4/	− 8.0

○ **Inconsistent** with Schwarzschild (GR BH in vac.),  
 $A \neq 0$ ,  $B \neq 1$  with **> 99.9% credibility**

# Preliminary

## ○ Marginal plots of some parameters

■ p16-p50   ■ p50-p84   - - - Schwarzschild (A,B)



◇ Our result indicates two+1 possibilities:

- If GR is correct, then the modelling of 2-body-system in “vacuum BH spacetime” is not good.

→ **Dark Matters accumulate at Sgr A\*!?**

- If the vac. BH environment is the good model, then a “modified gravity theory” is favored.
- Hybrid of the above possibilities.

# 4. Summary and Discussions

- Using the data of S-stars, Gravity/BH is tested.
- BH's mass effects are in our detection capability.
- Are “BH in vacuum” and/or “GR” credible?
- Bayesian-fitting of PPN BH with given data set

**GR BH in vacuum (Schwarzschild) is ruled out with more than 99.9% credibility.**

- ◇ **Dark Matter Accumulation around Sgr A\***
- ◇ **Violation of GR**

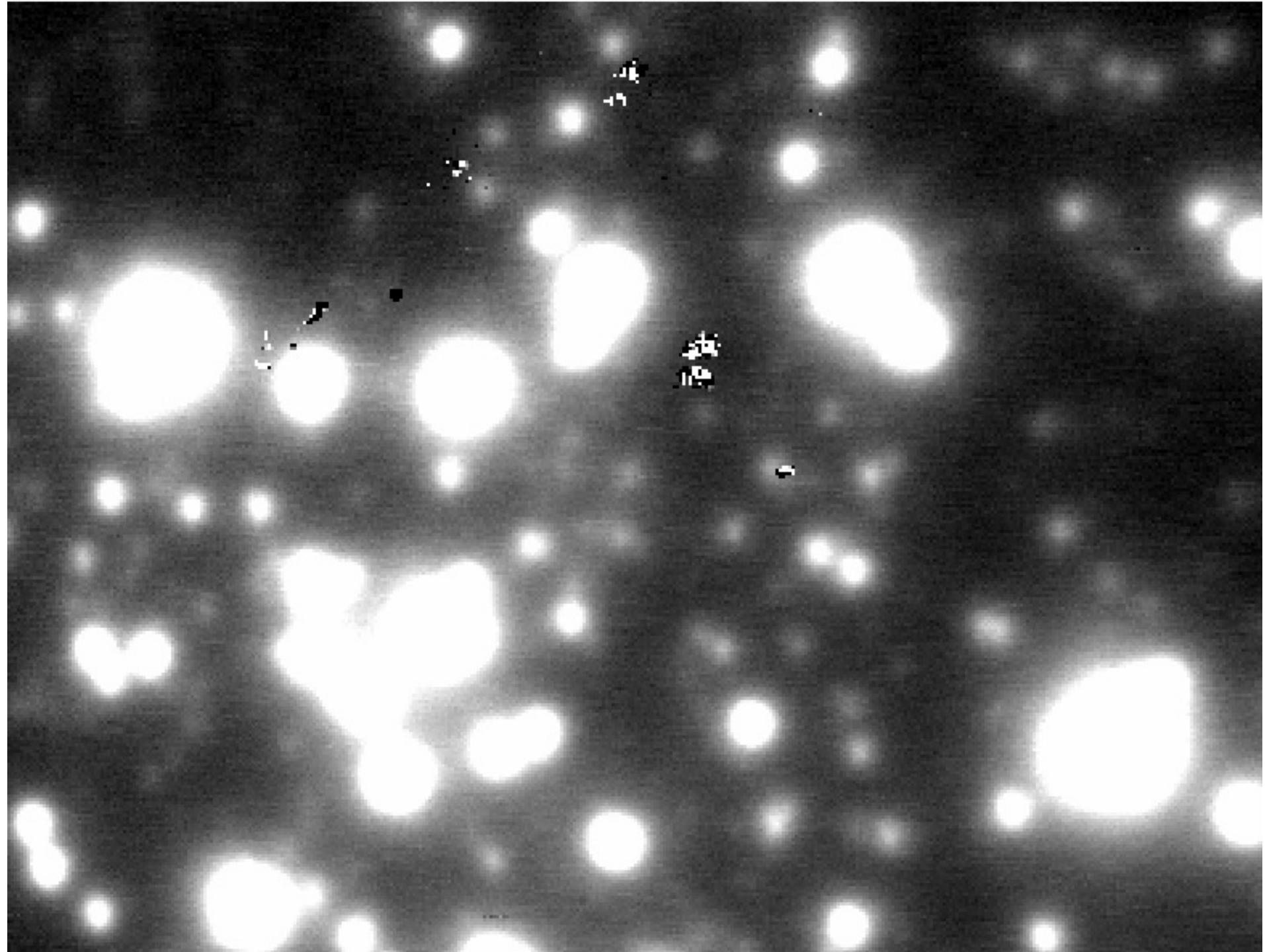
- Three discussions . . .

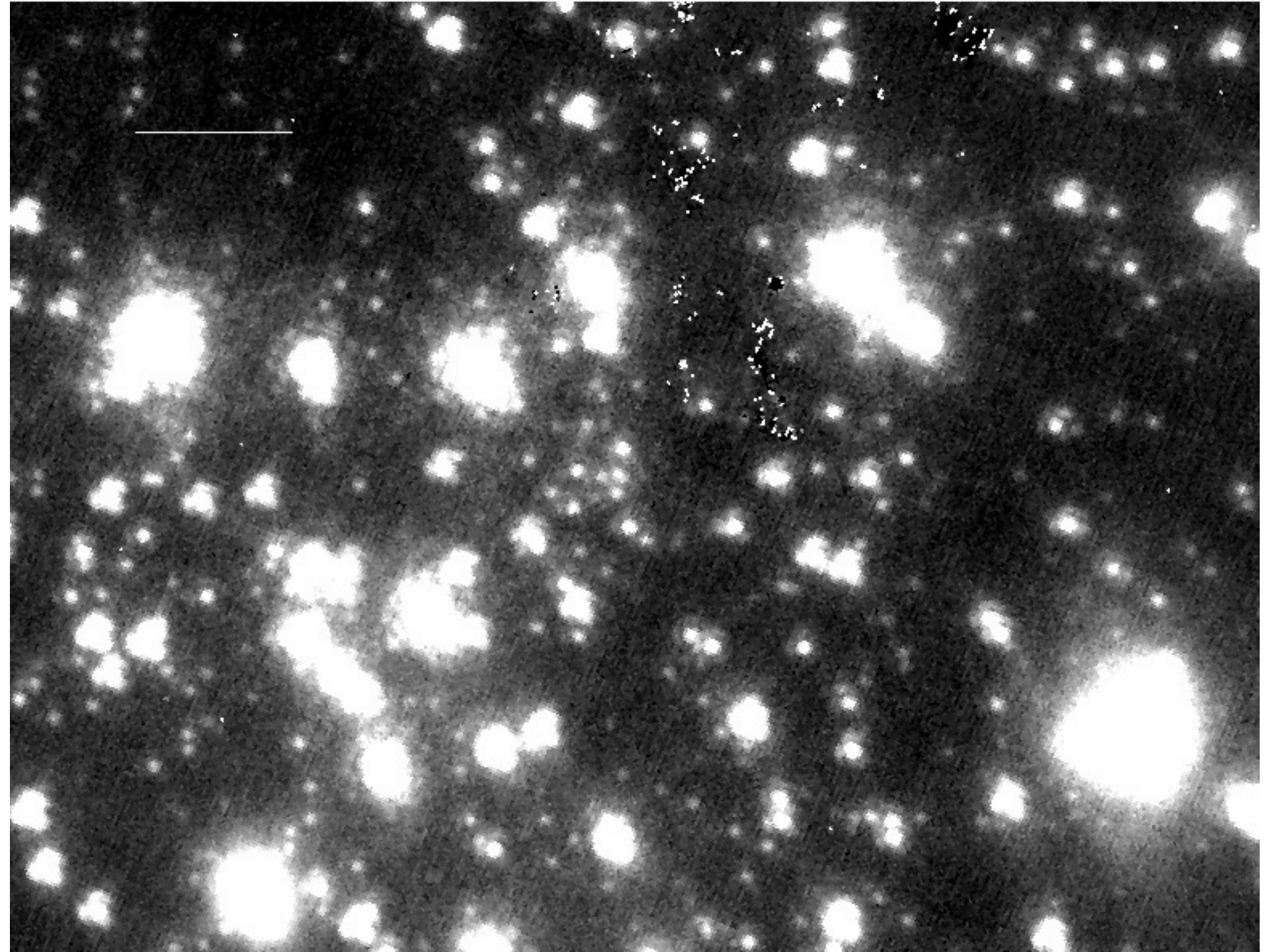
- ◇ Quantitative estimate of
  - { Amount of Dark Matters
  - { Modified Gravity Parameters

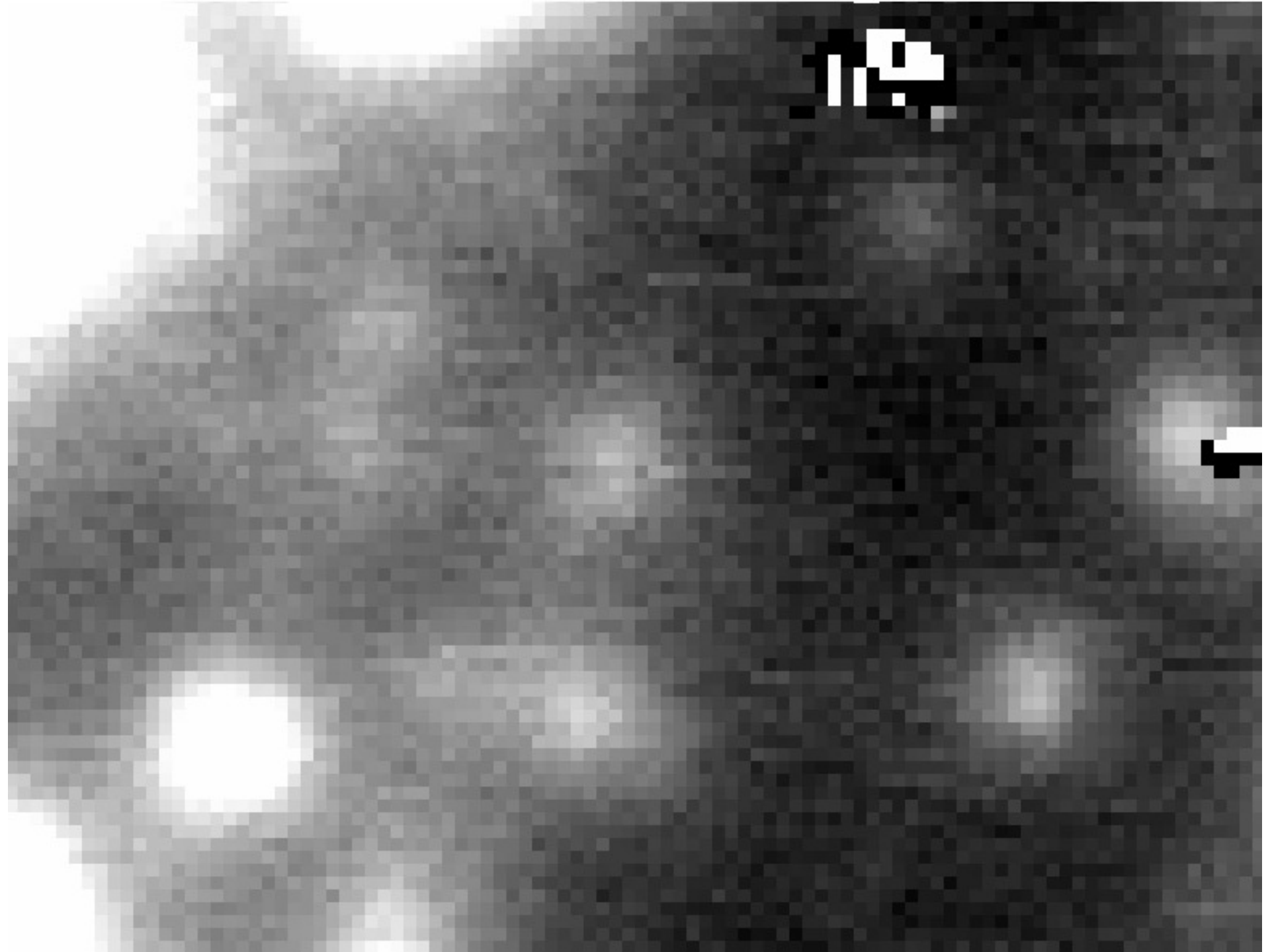
→ Under calculation using exact solutions of  
GR hairy BH and DHOST BH
- ◇ Comparison with GRAVITY group's result
  - They are doing a similar PPN analysis with
    - { very different data set
    - { different policy of parameter treatments
    - { NO gravitational lens effect
- ◇ Analysis of our data taken with NIR-WFS/AO3k

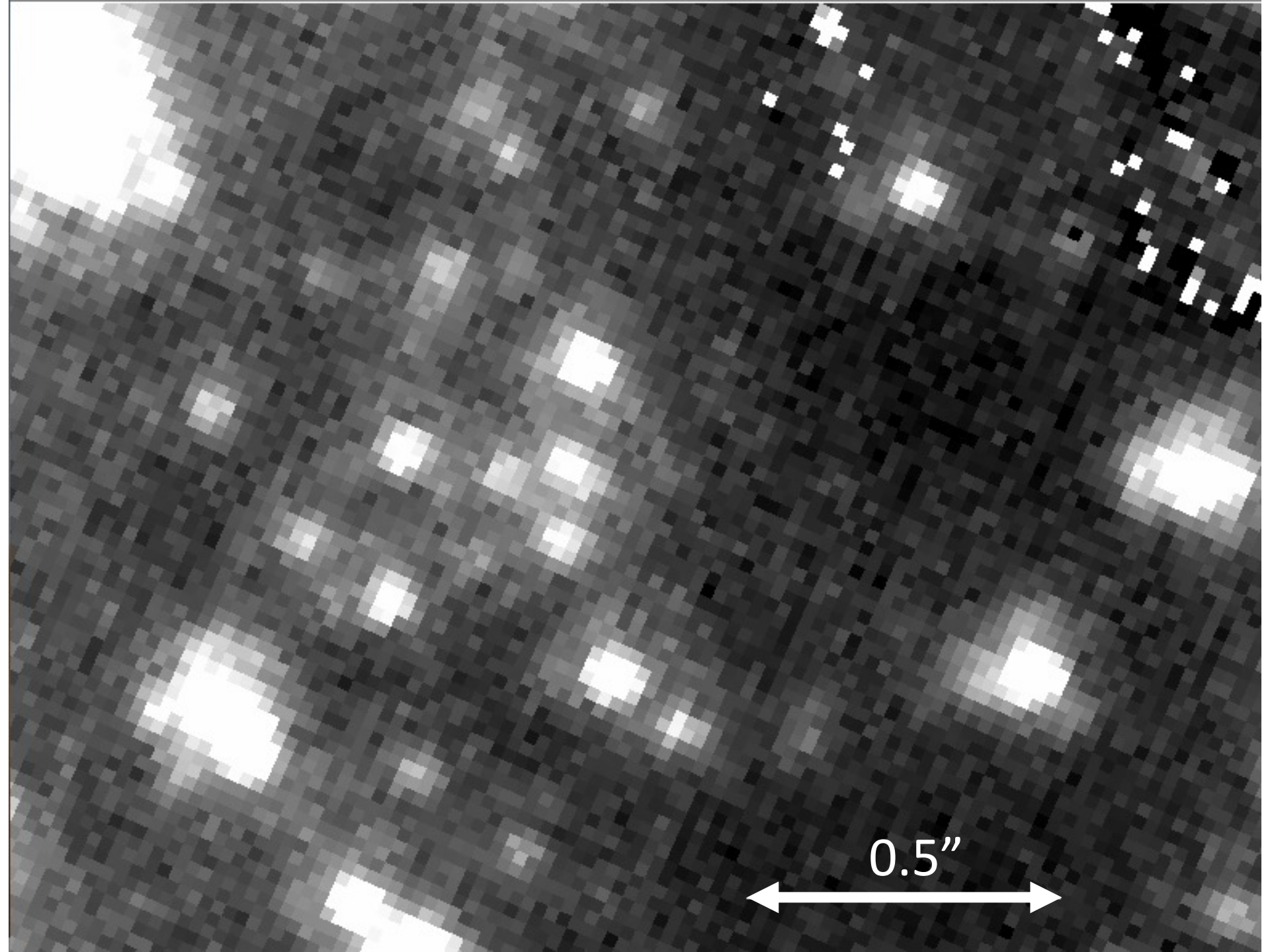
— **Supplement: NIR-WFS/A03k Data** —

Comparison of  
IRCS/A0188 with IRCS/NIR-WFS/A03k  
for NIR observaion of S-stars









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