

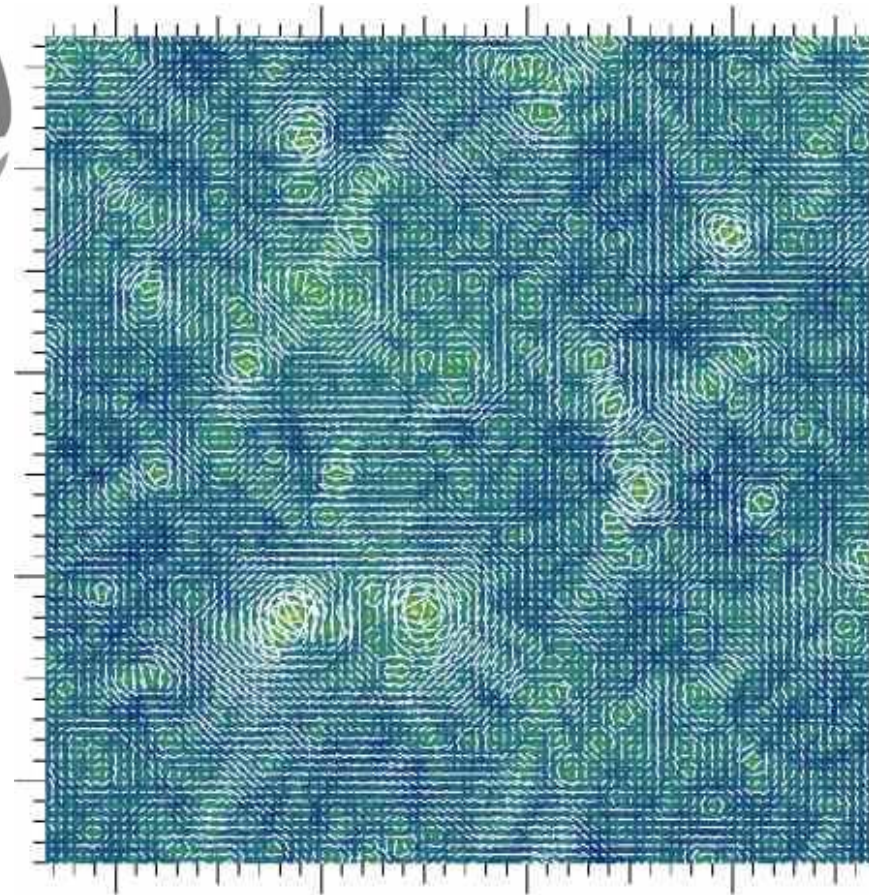
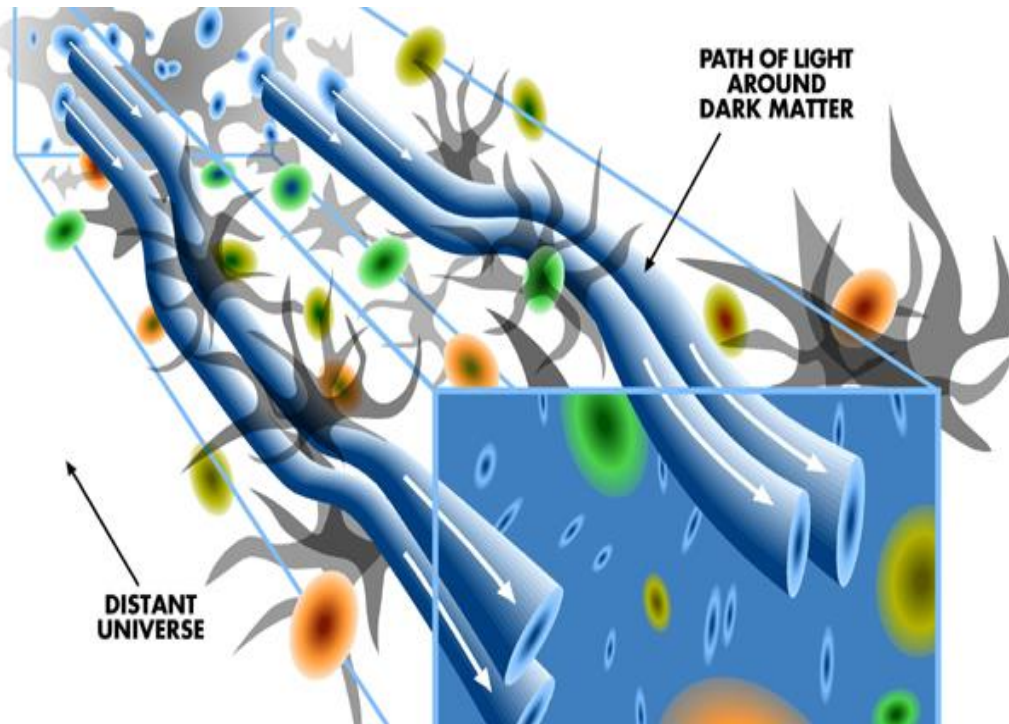
Explore Point Spread Function Combining Star and Galaxy Images

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Outlines

- Weak lensing background
- Basis function and PSF reconstruction
- Our new algorithm
- Testing
- Summary

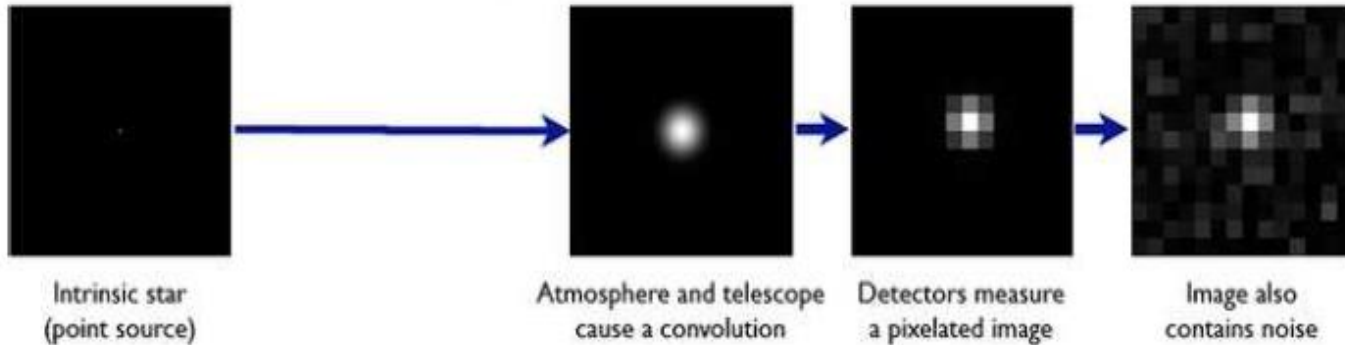
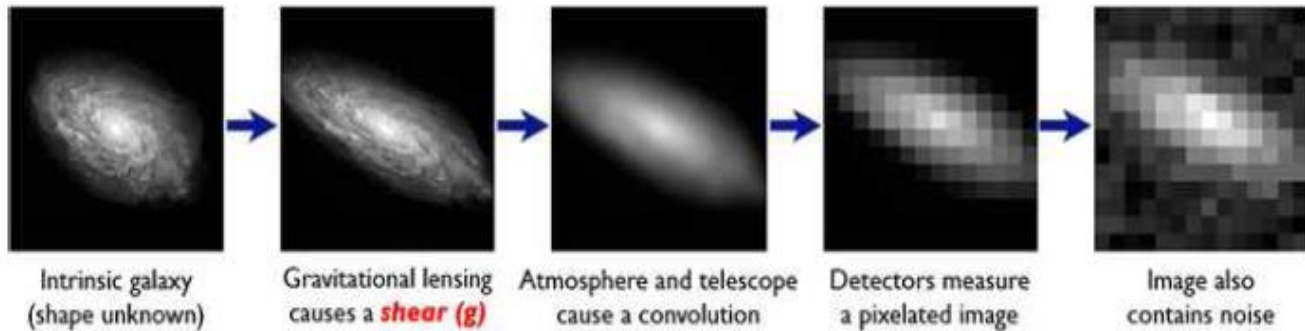
Weak lensing background



Point Spread Function

The Forward Process.

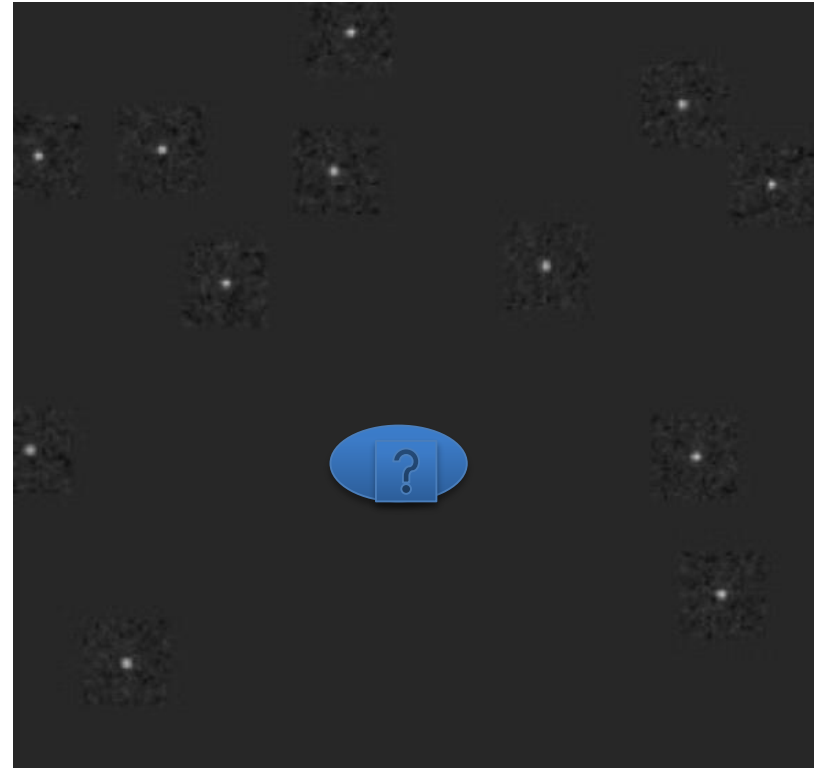
Galaxies: Intrinsic galaxy shapes to measured image:



Usually, the distortion introduced by PSF is larger than that caused by cosmic shear!

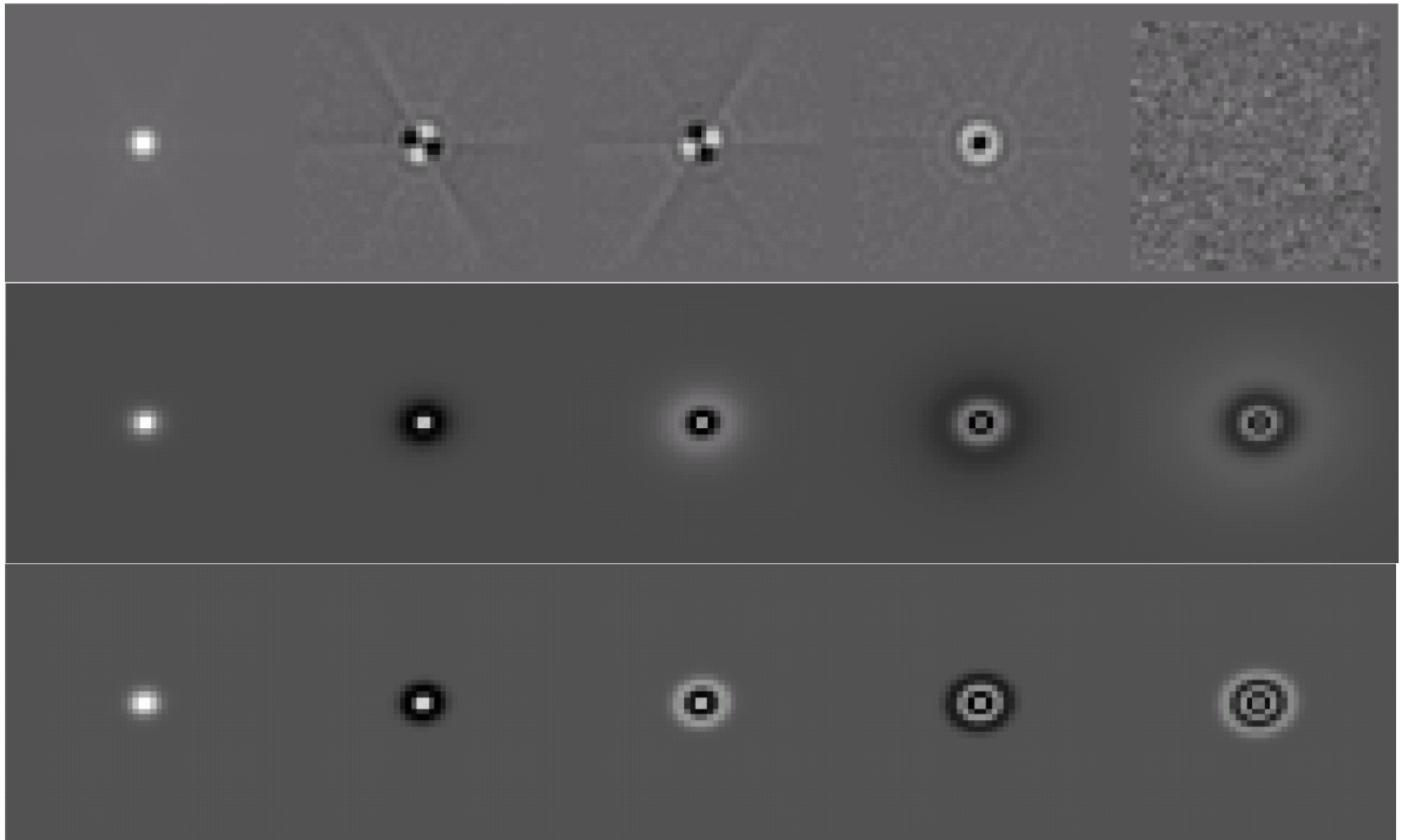
How do we do the reconstruction?

- A) Star identification.
- B) Parameterized image of stars.
- C) Interpolate the parameters in the field of view.
- D) Create the expected PSF at the position of galaxies.



Parameterization of PSF

PCA, Gaussianlets and Moffatlets



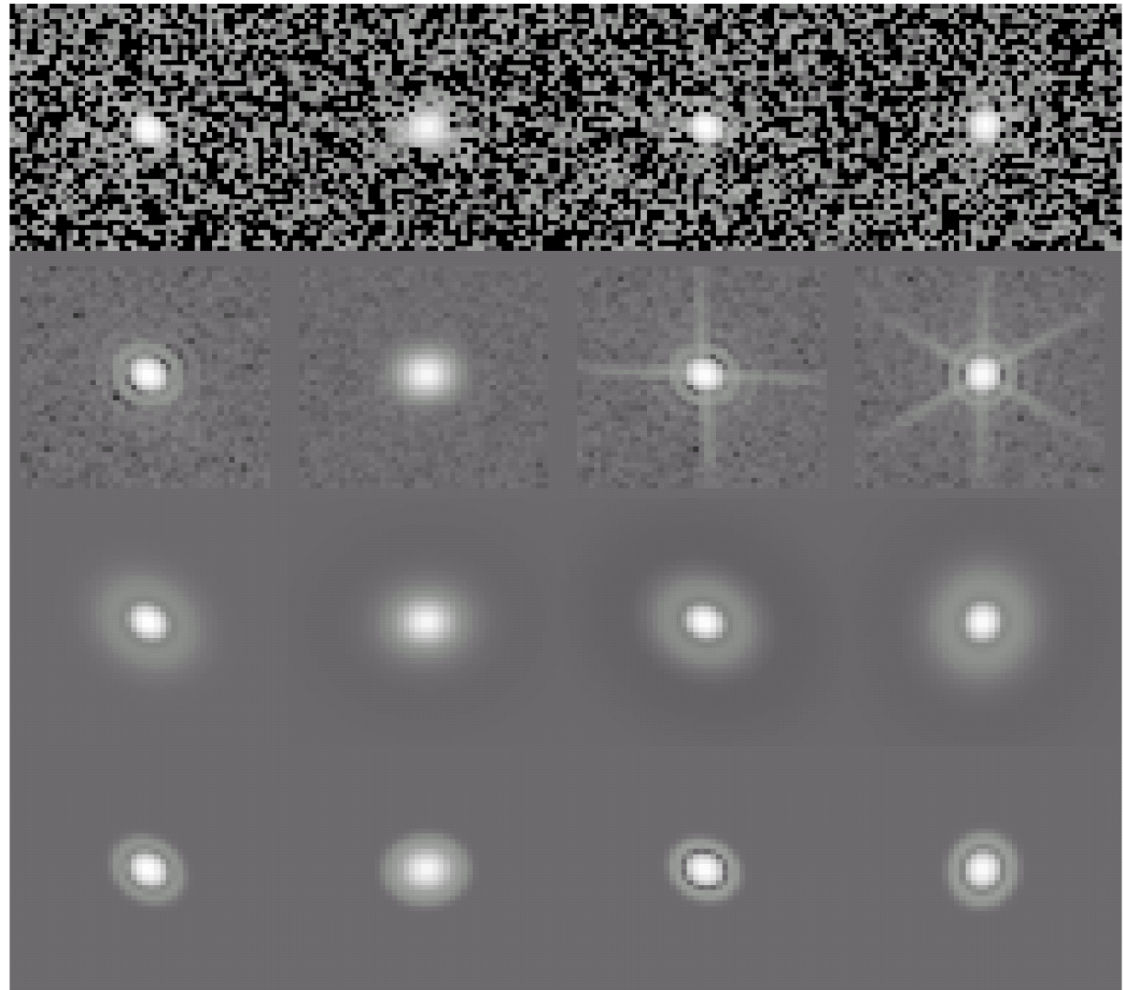
Test with GREAT10 data

One star in different
data set

Principal Component
Analysis (PCA)

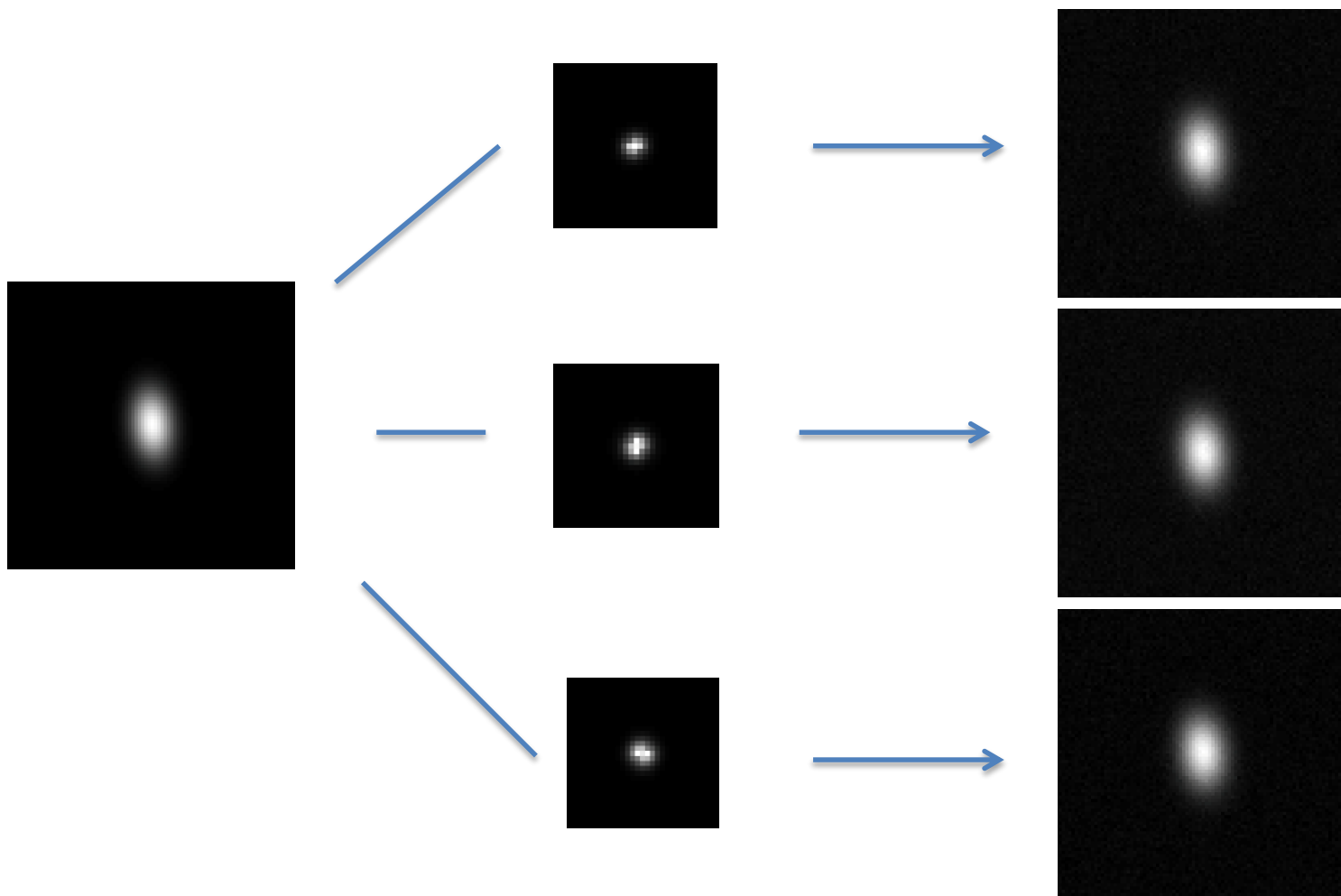
Moffatlets

Gaussianlets



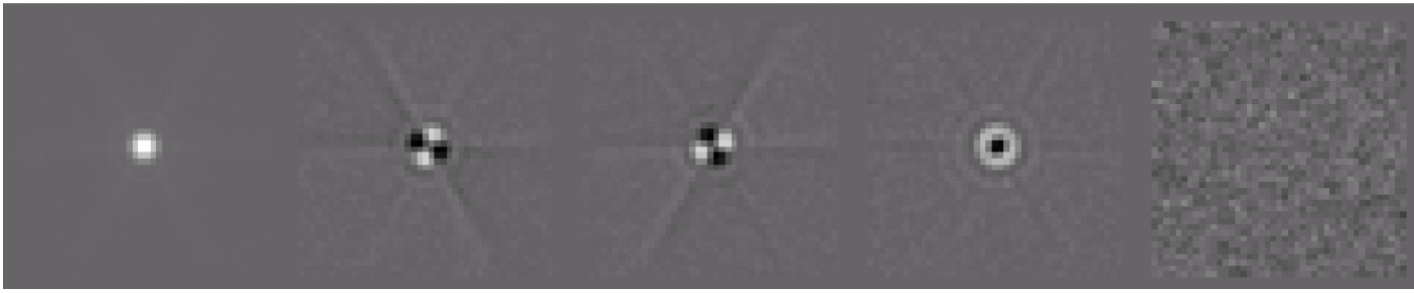
Motivation

- Interpolation doesn't always work when the number of star is too few or the PSF changes too fast in the field.
- Galaxy images themselves contain the local information of the PSF



Unknowns: $N_g \times N_g$ + $3 \times N_P \times N_P$

Knows: $3 \times N_g \times N_g$



The number of unknowns of PSF can decrease to several by using basis functions.


$$PSF_i = \sum_l^{N_{PC}} c_{il} PC_{il},$$

$$NPg \times NPg \rightarrow N_{PC}$$

$$G_0 \Delta PSF_i \Delta PSF_j = G_i \Delta PSF_j = G_j \Delta PSF_i = G_0 \Delta PSF_j \Delta PSF_i$$

$$c_{ij}^2 = \frac{1}{N_{pixel}} \sum_k \frac{(G_i \Delta PSF_j - G_j \Delta PSF_i)_k^2}{S_{ijk}^2}$$

Define $G_{ijl} = G_i \ddot{A} PC_{jl}$

$$c^2 = \ddot{a}_{i,j}^{N_{image}} \ddot{a}_k^{N_{pixel}} \frac{(\ddot{a}_{jl} c_{jl} G_{ijlk} - \ddot{a}_{il} c_{il} G_{jilk})^2}{S_{ijk}^2}$$


The minimization $\frac{\|\cdot\|^2}{\|c_{mn}\|} = 0$ leads

$$\ddot{a}_{ml}^{N_{PC}} \ddot{a}_i^{N_{image}} \ddot{a}_k^{N_{pixel}} \frac{G_{imnk} G_{imlk}}{S_{imk}^2} - \ddot{a}_{il}^{N_{PC}} \ddot{a}_i^{N_{image}} \ddot{a}_k^{N_{pixel}} \frac{G_{imnk} G_{milk}}{S_{imk}^2} = 0$$

With noise

$$G'_i = G_i + n_i$$

Define $n_{ij} = n_i \otimes PSF_j$

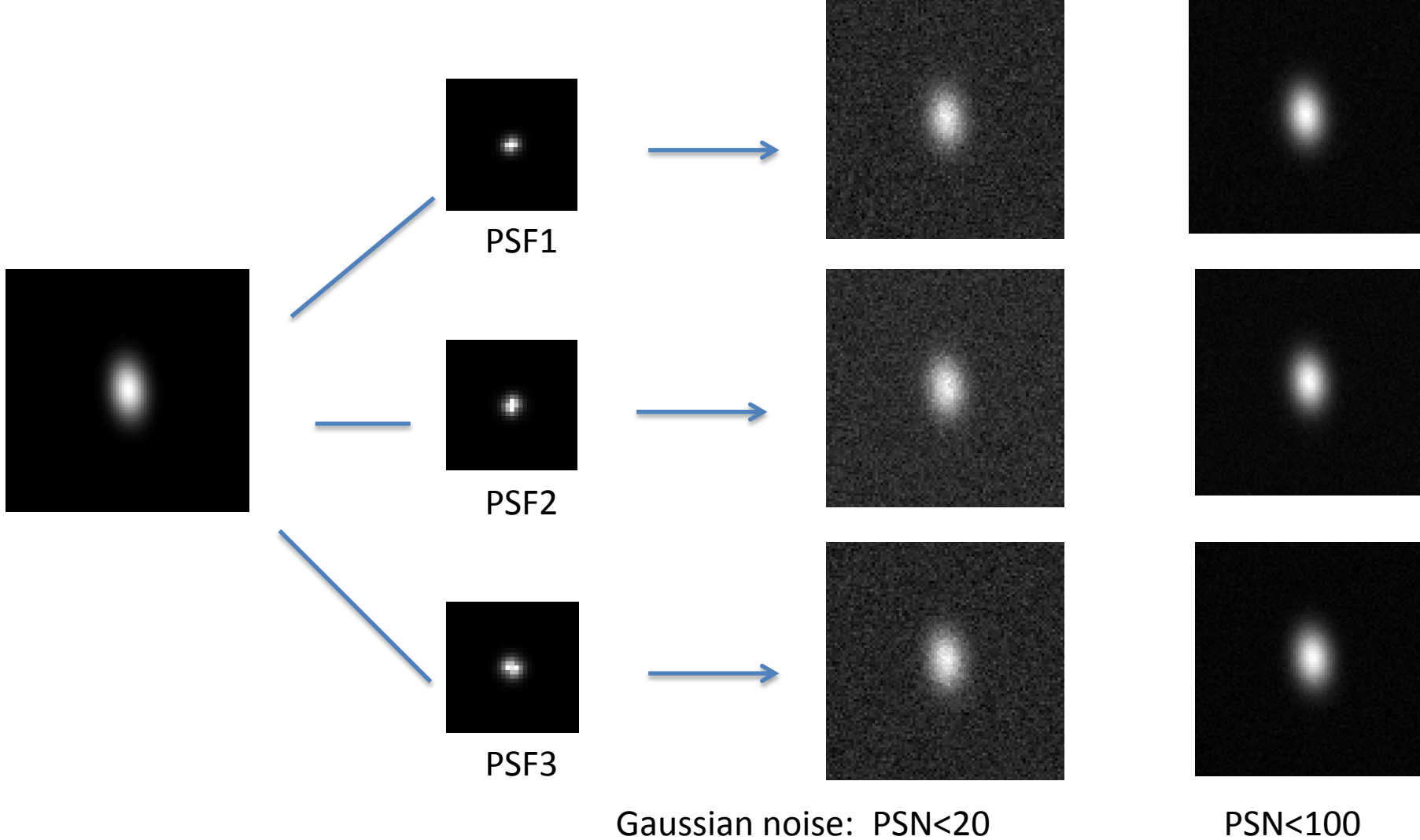
We get

$$C^2 @ \sum_{\substack{i,j \\ i^1 j}}^{N_{image}} \sum_k^{N_{pixel}} \frac{(\sum_l c_{jl} G_{ijlk} - \sum_l c_{il} G_{jilk})^2 + (n_{ijk} - n_{jik})^2}{S_{ijk}^2}$$

$$G_i \otimes PSF_j = G_j \otimes PSF_i \Rightarrow w' G_i \otimes PSF_j = w' G_j \otimes PSF_i$$

The final equation is:

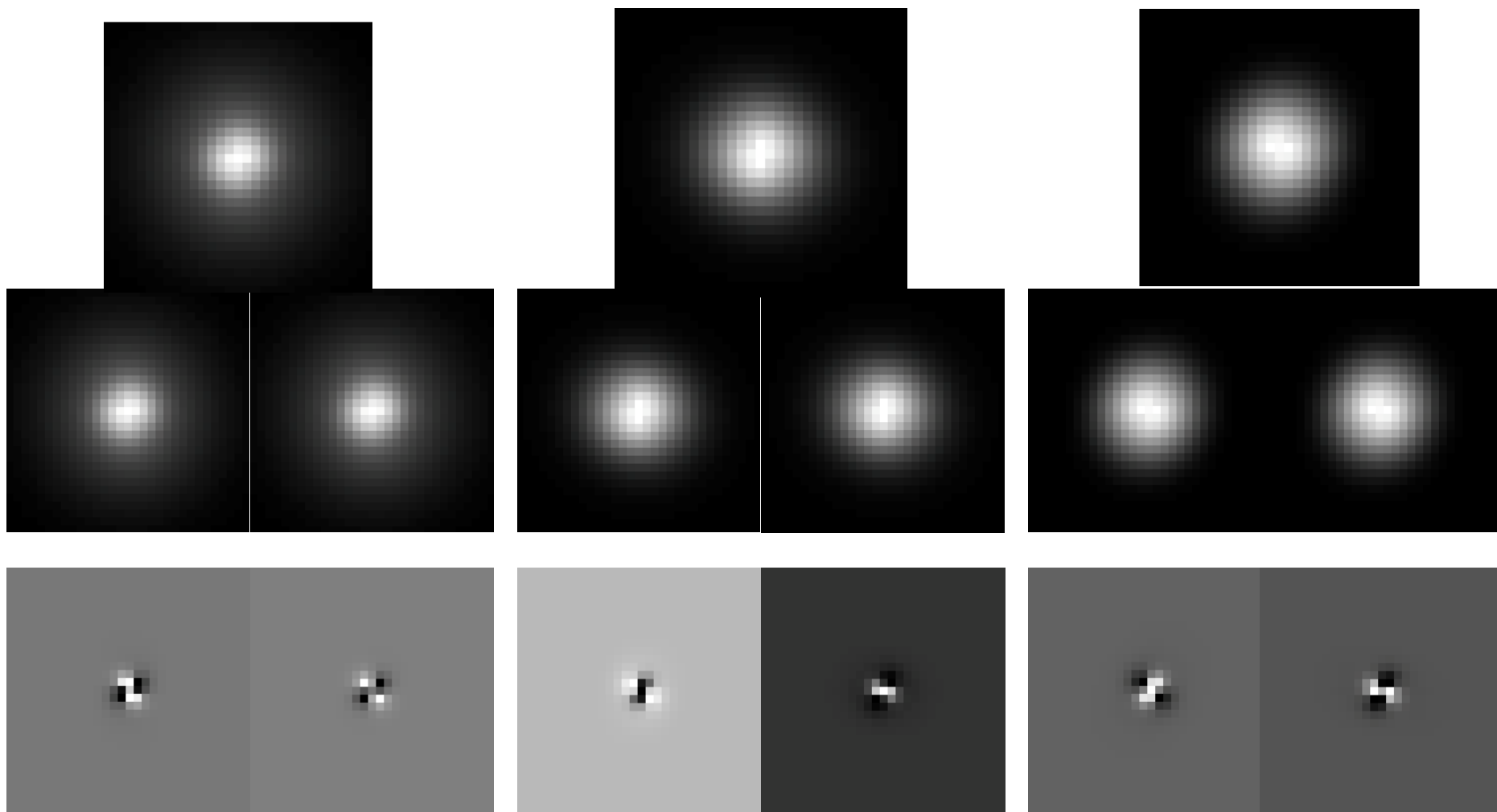
$$\sum_l^{N_{PC}} \sum_{\substack{i \\ i^1 m}}^{N_{image}} \sum_k^{N_{pixel}} \frac{w_k G'_{imnk} G'_{imlk}}{S_{imk}^2} - \sum_l^{N_{PC}} \sum_{\substack{i \\ i^1 m}}^{N_{image}} c_{il} \sum_k^{N_{pixel}} \frac{w_k G'_{imnk} G'_{milk}}{S_{imk}^2} = 0$$

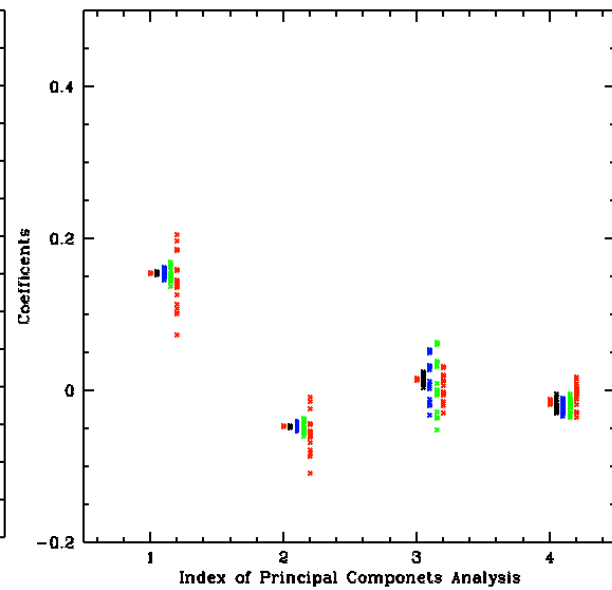
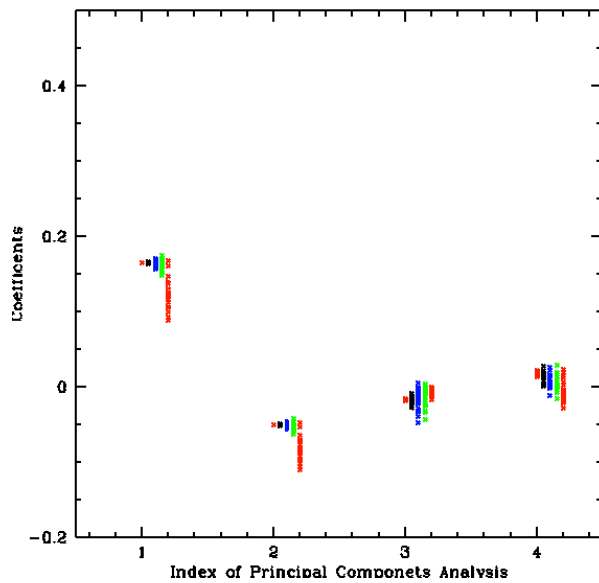
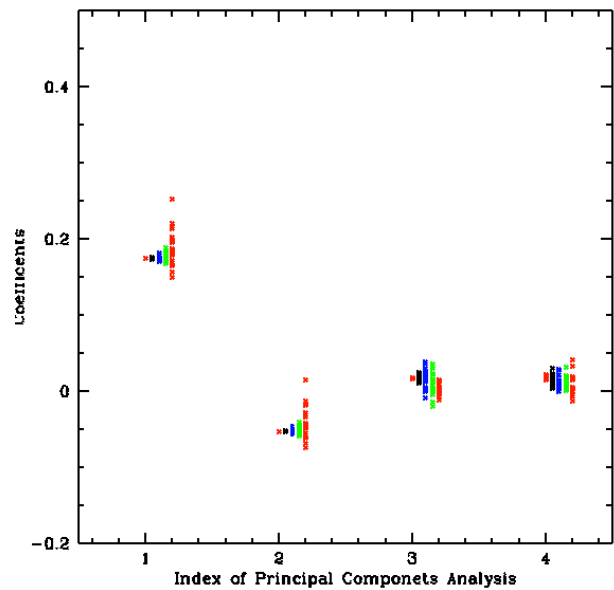
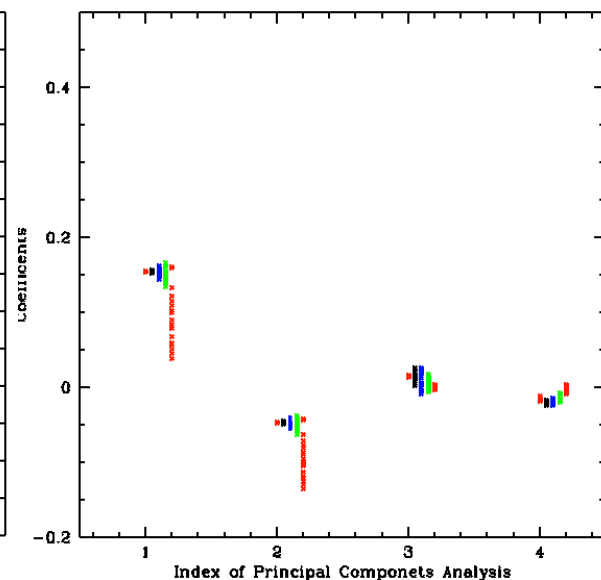
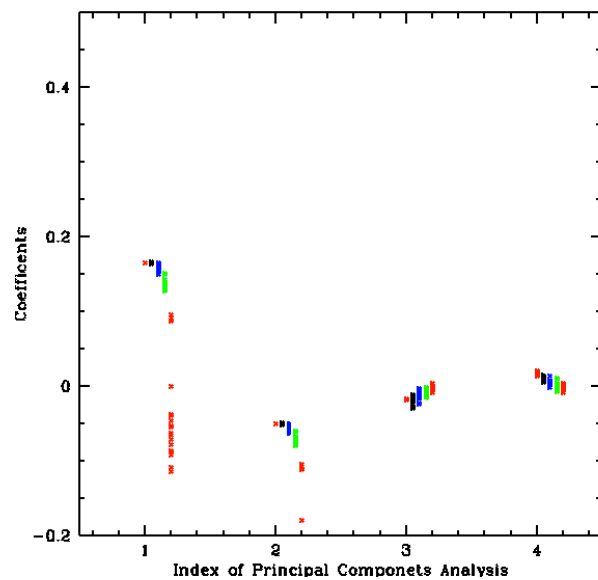
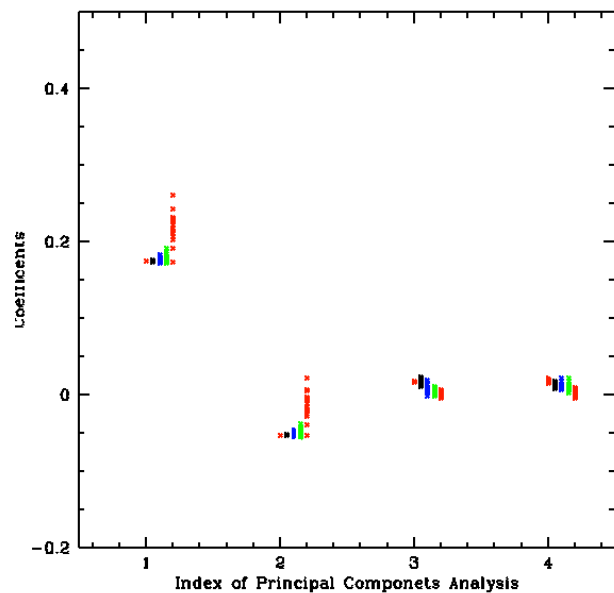


$$c_{11}x \text{ PC11} + c_{12}x \text{ PC12} + c_{13}x \text{ PC13} + c_{14}x \text{ PC14} = \text{PSF1}$$

The equation shows the linear combination of four principal components (PC11, PC12, PC13, PC14) with coefficients $c_{11}x$, $c_{12}x$, $c_{13}x$, and $c_{14}x$ to reconstruct the target PSF1. The components are shown as small images with their respective labels below them.

The Reconstructed PSFs





Summary

- It works!
- It needs multi-exposed images with **different** PSF.
- Principal Components Analysis of stars provides the most compact basis function .
- More tests needed: center disalignment, noise estimation of the cross-convolved images, incomplete PCs

Thanks